

## Second-Order Homogeneous Differential Equations with Constant Coefficients

1. Suppose  $f(t)$  and  $g(t)$  are both solutions to the differential equation  $y'' + by' + cy = 0$ . Is  $C_1f(t) + C_2g(t)$  a solution as well?
2. Can you guess solutions of  $y'' = y$ ? Try to guess two solutions that are not just multiples of each other.
3. Can you guess solutions of  $y'' = 4y$ ? Try to guess two solutions that are not just multiples of each other.
4. Solve  $y'' - y' = 6y$ .

5. Solve  $y'' + 5y' + 4y = 0$  where  $y(0) = 1$  and  $y'(0) = 2$ .

6. Solve  $y'' - 4y' + 4y = 0$ .

7. Show that, if the characteristic equation  $y'' + by' + cy = 0$  has one repeated root  $r$ , then  $y = te^{rt}$  is a solution to  $y'' + by' + cy = 0$ .