

LET  $\vec{X} = (x_1, x_2, \dots, x_N)$  AND  $\vec{Y} = (y_1, y_2, \dots, y_N)$ .

THEN  $M_x = \frac{x_1 + x_2 + \dots + x_N}{N}$  AND  $M_y = \frac{y_1 + y_2 + \dots + y_N}{N}$

ARE THE MEANS OF  $\vec{X}$  AND  $\vec{Y}$ , RESPECTIVELY.

$$\begin{aligned} SD_x &= \frac{1}{\sqrt{N}} \sqrt{(x_1 - M_x)^2 + (x_2 - M_x)^2 + \dots + (x_N - M_x)^2} \\ &= \frac{1}{\sqrt{N}} \|\vec{X} - M_x(1, 1, \dots, 1)\| \quad \text{AND} \end{aligned}$$

$$\begin{aligned} SD_y &= \frac{1}{\sqrt{N}} \sqrt{(y_1 - M_y)^2 + (y_2 - M_y)^2 + \dots + (y_N - M_y)^2} \\ &= \frac{1}{\sqrt{N}} \|\vec{Y} - M_y(1, 1, \dots, 1)\| \end{aligned}$$

ARE THE STANDARD DEVIATIONS OF  $\vec{X}$  AND  $\vec{Y}$ , RESPECTIVELY.

RULE OF THUMB - FOR MOST VECTORS  $\vec{X}$  AT LEAST 68% OF THE ENTRIES WILL LIE BETWEEN  $M_x - SD_x$  AND  $M_x + SD_x$ , WHILE AT LEAST 95% WILL LIE BETWEEN  $M_x - 2SD_x$  AND  $M_x + 2SD_x$ .

THE LEAST SQUARES LINE (OFTEN CALLED THE BEST FIT LINE OR THE REGRESSION LINE) FOR  $(x_1, y_1), (x_2, y_2), \dots, (x_N, y_N)$  IS THE LINE WHICH MINIMIZES THE SUM OF THE SQUARES OF THE VERTICAL DISTANCES FROM THE POINTS TO THE LINE. IF  $y = bx + a$  IS THE LEAST SQUARES LINE, WE FIND A AND B