

## SUMMARY OF SECTION 2.4

IF  $A$  IS A SQUARE MATRIX, THEN THE MINOR OF  $a_{ij}$  IS DENOTED  $M_{ij}$  AND IS DEFINED TO BE THE DETERMINANT OF THE SUBMATRIX THAT REMAINS AFTER THE  $i^{\text{TH}}$  ROW AND  $j^{\text{TH}}$  COLUMN ARE DELETED FROM  $A$ . THE NUMBER  $(-1)^{i+j} M_{ij}$  IS DENOTED BY  $C_{ij}$  AND IS CALLED THE COFACTOR OF  $a_{ij}$ .

CALCULATING  $\text{DET}(A)$  BY COFACTOR EXPANSION:

$$\rightarrow \text{DET}(A) = a_{1j} C_{1j} + a_{2j} C_{2j} + \dots + a_{nj} C_{nj}$$

(EXPANSION ALONG THE  $j^{\text{TH}}$  COLUMN)

$$\rightarrow \text{DET}(A) = a_{i1} C_{i1} + a_{i2} C_{i2} + \dots + a_{in} C_{in}$$

(EXPANSION ALONG THE  $i^{\text{TH}}$  ROW)

IF  $A$  IS AN  $N \times N$  MATRIX, THEN CALLED THE MATRIX OF COFACTORS FROM  $A$ .

$$\begin{bmatrix} C_{11} & C_{12} & \dots & C_{1N} \\ C_{21} & C_{22} & \dots & C_{2N} \\ \vdots & \vdots & \ddots & \vdots \\ C_{N1} & C_{N2} & \dots & C_{NN} \end{bmatrix} \text{ IS}$$

THE TRANSPOSE OF THIS MATRIX IS CALLED THE ADJOINT OF  $A$  AND IS DENOTED  $\text{ADJ}(A)$ .

THEOREM - IF  $A$  IS INVERTIBLE, THEN

$$A^{-1} = \frac{1}{\text{DET}(A)} \text{ADJ}(A).$$