

1.2 # 6

A)
$$\begin{bmatrix} 1 & 1 & 2 & 8 \\ -1 & -2 & 3 & 1 \\ 3 & -7 & 4 & 10 \end{bmatrix} \xrightarrow[\text{SUB } 3 \text{ (1) FROM (3)}]{\text{ADD (1) TO (2)}} \begin{bmatrix} 1 & 1 & 2 & 8 \\ 0 & -1 & 5 & 9 \\ 0 & -10 & -2 & -14 \end{bmatrix}$$

$$\xrightarrow[\text{MULT (2) BY } -1]{\text{SUB } 10 \text{ (2) FROM (3)}} \begin{bmatrix} 1 & 1 & 2 & 8 \\ 0 & 1 & -5 & -9 \\ 0 & 0 & -52 & -104 \end{bmatrix} \xrightarrow[\text{MULT (3) BY } \frac{-1}{52}]{\text{SUB (1) FROM (2)}} \begin{bmatrix} 1 & 0 & 7 & 17 \\ 0 & 1 & -5 & -9 \\ 0 & 0 & 1 & 2 \end{bmatrix}$$

$$\xrightarrow[\text{ADD } 5 \text{ (3) TO (2)}]{\text{SUB } 7 \text{ (3) FROM (1)}} \begin{bmatrix} 1 & 0 & 0 & 3 \\ 0 & 1 & 0 & 1 \\ 0 & 0 & 1 & 2 \end{bmatrix} \text{ So } x_1 = 3, x_2 = 1 \text{ AND } x_3 = 2$$

B)
$$\begin{bmatrix} 2 & 2 & 2 & 0 \\ -2 & 5 & 2 & 1 \\ 8 & 1 & 4 & -1 \end{bmatrix} \xrightarrow[\text{SUB } 4 \text{ (1) FROM (3)}]{\text{ADD (1) TO (2)}} \begin{bmatrix} 2 & 2 & 2 & 0 \\ 0 & 7 & 4 & 1 \\ 0 & -7 & -4 & -1 \end{bmatrix}$$

$$\xrightarrow{\text{ADD (2) TO (3)}} \begin{bmatrix} 2 & 2 & 2 & 0 \\ 0 & 7 & 4 & 1 \\ 0 & 0 & 0 & 0 \end{bmatrix} \xrightarrow[\text{MULT (2) BY } \frac{1}{7}]{\text{MULT (1) BY } \frac{1}{2}} \begin{bmatrix} 1 & 1 & 1 & 0 \\ 0 & 1 & \frac{4}{7} & \frac{1}{7} \\ 0 & 0 & 0 & 0 \end{bmatrix}$$

$$\xrightarrow{\text{SUB (2) FROM (1)}} \begin{bmatrix} 1 & 0 & \frac{3}{7} & -\frac{1}{7} \\ 0 & 1 & \frac{4}{7} & \frac{1}{7} \\ 0 & 0 & 0 & 0 \end{bmatrix} \text{ So } \begin{aligned} x_3 &= T \\ x_1 &= -\frac{1}{7} - \frac{3}{7}T \\ x_2 &= \frac{1}{7} - \frac{4}{7}T \end{aligned}$$

C)
$$\begin{bmatrix} 1 & -1 & 2 & -1 & -1 \\ 2 & 1 & -2 & -2 & -2 \\ -1 & 2 & -4 & 1 & 1 \\ 3 & 0 & 0 & -3 & -3 \end{bmatrix} \xrightarrow[\text{SUB } 3 \text{ (1) FROM (4)}]{\text{SUB } 2 \text{ (1) FROM (2) AND ADD (1) TO (2)}} \begin{bmatrix} 1 & -1 & 2 & -1 & -1 \\ 0 & 3 & -6 & 0 & 0 \\ 0 & 1 & -2 & 0 & 0 \\ 0 & 3 & -6 & 0 & 0 \end{bmatrix}$$

NOTE: IT MIGHT BE MORE SIMPLE TO START BY INTERCHANGING ROWS 1 AND 4.