

$$24 \quad f(x,y) = x^2 - xy + 3y^2 \quad (3,-1) \text{ to } (2.96, -0.95)$$

$$f(3,-1) = 15$$

$$f(2.96, -0.95) = 14.2811$$

$$\Delta Z = -0.7189$$

$$f_x = 2x - y \quad f_y = 6y - x$$

$$f_x(3,-1) = 7$$

$$f_y(3,-1) = -9$$

$$dz = f_x dx + f_y dy = 7(x-x_0) - 9(y-y_0)$$
$$= 7(-0.04) - 9(+0.05) = -0.73$$

$$dz = -0.73$$

$$\Delta Z = -0.7189$$

30.

$$P = \frac{8.31 T}{V}$$

$$dP = \frac{dP}{dT} dT + \frac{dP}{dV} dV$$

$$= \frac{8.31}{V} dT + \left(-\frac{8.31 T}{V^2} \right) dV$$

$$dT = 305 - 310 = -5$$

$$dV = 12.3 - 12 = 0.3$$

$$dP = \frac{8.31}{12} (-5) - \frac{8.31(310)}{(12)^2} (0.3)$$

$$dP = -8.829$$