

$$16. \quad \|u+v\|^2 + \|u-v\|^2 = 2\|u\|^2 + 2\|v\|^2$$

$$\|u+v\|^2 = (u+v) \cdot (u+v) = u \cdot u + u \cdot v + v \cdot u + v \cdot v = \|u\|^2 + 2(u \cdot v) + \|v\|^2$$

$$\|u-v\|^2 = (u-v) \cdot (u-v) = u \cdot u - u \cdot v - v \cdot u + v \cdot v = \|u\|^2 - 2(u \cdot v) + \|v\|^2$$

So clearly, by adding $\|u+v\|^2$ to $\|u-v\|^2$, the result is $2\|u\|^2 + 2\|v\|^2$.

$$22. \quad v \cdot (k_1 w_1 + k_2 w_2) = k_1 \underbrace{(v \cdot w_1)}_0 + k_2 \underbrace{(v \cdot w_2)}_0 = 0. \quad \checkmark$$