

$$13. f(x,y) = \sqrt{20-x^2-7y^2}, (2,1)$$

$$f(2,1) = 3$$

$$f_x = \frac{-x}{\sqrt{20-x^2-7y^2}} \quad f_y = \frac{-7y}{\sqrt{20-x^2-7y^2}}$$

$$f_x(2,1) = -\frac{2}{3} \quad f_y(2,1) = -\frac{7}{3}$$

$$L(x,y) = 3 - \frac{2}{3}(x-2) - \frac{7}{3}(y-1) \\ = -\frac{2}{3}x - \frac{7}{3}y + \frac{20}{3}$$

$$L(1.99, 1.08) = 2.846$$

$$20. v = y \cos xy$$

$$v_x = -y^2 \sin xy \quad v_y = -xy \sin xy + \cos xy$$

$$dv = -y^2 \sin xy \, dx + (-xy \sin xy + \cos xy) \, dy$$

$$22. u = \frac{r}{s+2t}$$

$$du = u_r \, dr + u_s \, ds + u_t \, dt$$

$$u_r = \frac{1}{s+2t} \quad u_s = \frac{-r}{(s+2t)^2} \quad u_t = \frac{-2r}{(s+2t)^2}$$

$$du = \frac{dr}{s+2t} - \frac{r \, ds}{(s+2t)^2} - \frac{2r \, dt}{(s+2t)^2}$$