

$$9a. \quad u \cdot (7v+w) = (3,4) \cdot [(35,-7) + (7,1)] = (3,4) \cdot (42,-6) = 126 - 24 = 102$$

$$b. \quad \|(u \cdot w)u\| = \|(3 \cdot 7 + 4 \cdot 1)(7,1)\| = \|(25)(7,1)\| = (25)\|(7,1)\| = 25\sqrt{(49)+1} = 25\sqrt{50} = 125\sqrt{2}.$$

$$c. \quad \|u\| (v \cdot w) = (\sqrt{3^2+4^2})(5 \cdot 7 + (-1) \cdot 6) = (5)(34) = 170$$

$$d. \quad (\|u\|v) \cdot w = (25,-5) \cdot (7,1) = 25 \cdot 7 - 5 \cdot 1 = 175 - 5 = 170.$$

12. These points are not colinear, so they form a triangle.

$$\vec{AB} = (4-3, 3-0, 0-2) = (1, 3, -2)$$

$$\vec{BC} = (8-4, 1-3, -1-0) = (4, -2, -1)$$

$$\vec{AB} \cdot \vec{BC} = 1 \cdot 4 - 3 \cdot 2 + 2 \cdot 1 = 4 - 6 + 2 = 0, \text{ so } \vec{AB} \text{ and } \vec{BC} \text{ are orthogonal, so there is a right angle at the vertex B.}$$

13. Find a unit vector  $w$  orthogonal to  $u = (1, 0, 1)$  and  $v = (0, 1, 1)$ .

$$w = (x, y, z)$$

$$u \cdot w = 0 \Rightarrow x + z = 0 \Rightarrow x = -z$$

$$v \cdot w = 0 \Rightarrow y + z = 0 \Rightarrow y = -z$$

$$\text{So, } w = (x, x, -x). \quad \|w\| = \sqrt{(x^2) + x^2 + (-x)^2} = \pm x\sqrt{3}$$

$$\text{So the unit vector is } \left(\frac{1}{\sqrt{3}}, \frac{1}{\sqrt{3}}, \frac{-1}{\sqrt{3}}\right) \text{ or } \left(\frac{-1}{\sqrt{3}}, \frac{-1}{\sqrt{3}}, \frac{1}{\sqrt{3}}\right)$$

14) a. If  $p+q$  are  $\parallel$ , if 3 is  $\frac{3}{2}$  of 2, 5 is  $\frac{3}{2}$  of  $k$ . So,  $k = \frac{10}{3}$

$$b. \quad p \cdot q = 0 \Rightarrow 2 \cdot 6 + k \cdot 5 = 0 \Rightarrow k = -\frac{6}{5}$$

$$c. \quad \cos \frac{\pi}{3} = \frac{1}{2} = \frac{p \cdot q}{\|p\| \|q\|} = \frac{6+5k}{(\sqrt{4+k^2})(\sqrt{34})} \quad \text{Simplified, } k = \frac{-60+34\sqrt{3}}{33}$$

$$d. \quad \cos \frac{\pi}{4} = \frac{\sqrt{2}}{2} = \frac{6+5k}{(\sqrt{4+k^2})(\sqrt{34})} \quad \text{Simplified, } k = \frac{1}{2}$$