

## ANSWERS:

1. a)  $x - (2 - 2y + y^2)^{1/4} = 0$   
b)  $(x^2 + 4)^{1/2} - 2y = 0.$   
c)  $x^2/16 + y^2/9 = 1.$
2. a)  $x = 1.$   
b)  $27x + 4y = -73.$   
c)  $x + 3y = -1.$
3.  $e^2 + 1.$
4. a)  $(t \cos(t^3), t \sin(t^3)).$   
b)  $x \sin((x^2 + y^2)^{3/2}) - y \cos((x^2 + y^2)^{3/2}) = 0.$
5. a)  $\mathbf{B} = 1/3 \mathbf{A} + 1/3 (2, 4, -5).$   
b)  $\mathbf{B} = 11/25 \mathbf{A} + 1/25 (92, 69, 25).$   
c)  $\mathbf{B} = -1/3 \mathbf{A} + 1/3 (11, 8, 7).$
6. Only in Case c) are  $\mathbf{v}$  and  $\mathbf{w}$  perpendicular.
7. a)  $2/3.$   
b)  $(13)^{1/2}/7 .$
8. a)  $2x + y - z = 2.$   
b)  $x + y - z = 3.$   
c)  $x - y = -1.$
9.  $6/7.$
10.  $t \rightarrow (t, t, t)$  or  $t \rightarrow (-t, -t, -t).$
11. a) Yes. b) No. c) Yes. The answer is yes if there is a constant, non-zero vector which is orthogonal to  $\mathbf{v}$  at each time  $t$ . Otherwise, the answer is no. For a), consider  $(-1, 0, 5)$  and for c), consider  $(0, 7, 1)$ . No such vector exists for b) since in this case,  $\mathbf{v}(0) = (0, 0, 1)$  and so such a vector would have to lie in the  $x$ - $y$  plane. But then it couldn't be simultaneously orthogonal to  $\mathbf{v}(\pi/2)$  and  $\mathbf{v}(-\pi/2)$ .
12. a) In the first case,  $L = 20x + y - z - 9$ . In the second,  $L = 20x - y + 3z - 7$ .  
b) In the first case,  $L = z$ . In the second,  $L = 3y + z$ .