

1. Generalities about the importance of proofs. Induction.
2. Sets and maps $f : A \rightarrow B$ between sets [=functions], Id map, injective, surjective and bijective maps, the set $Maps(A, B)$.
3. The definition of composition $f \circ g \in Maps(A, C)$ for $f \in Maps(B, C)$, $g \in Maps(A, B)$.
4. Associativity and the lack of the commutativity.
5. The definition of the inverse map $f^{-1} \in Maps(B, A)$ for $f : A \rightarrow B$, the uniqueness of f^{-1} , the formula for $(f \circ g)^{-1}$, the criterion for the existence of inverse.
6. Automorphisms of a set. The difference between a finite and infinite sets. [If A is finite and $f : A \rightarrow A$ is an injective then f is an isomorphism.]
7. The definition of the symmetric group S_n , a way to write elements of S_n , elementary transpositions $s_i \in S_n$, $1 \leq i \leq n - 1$, the notions of a length $l(\sigma)$ of a permutations $\sigma \in S_n$.
8. Theorem. a) Any permutation σ can be written as a composition of elementary transpositions.
b) The smallest number of transpositions needed for a presentations of σ is equal to the length of σ .