

Problems for Gateway #1: Inequalities

1. The numerical values denoted by the inequality $-1 < x < 4$ consist of:
 - (a) all values of x between $x = -1$ and $x = 4$, including $x = -1$ but not $x = 4$
 - (b) all values of x between $x = -1$ and $x = 4$, including $x = 4$ but not $x = -1$
 - (c) all values of x between $x = -1$ and $x = 4$, including neither $x = -1$ nor $x = 4$
 - (d) all values of x between $x = -1$ and $x = 4$, including both $x = -1$ and $x = 4$
 - (e) all values of x that are less than $x = -1$ and all values of x that are greater than $x = 4$

2. The numerical values denoted by the inequality $2 \leq x < 5$ consist of:
 - (a) all values of x that are less than or equal to $x = 2$ and all values of x that are greater than 5 , but not including $x = 5$
 - (b) all values of x between $x = 2$ and $x = 5$, including both $x = 2$ and $x = 5$
 - (c) all values of x between $x = 2$ and $x = 5$, including neither $x = 2$ nor $x = 5$
 - (d) all values of x between $x = 2$ and $x = 5$, including $x = 2$ but not $x = 5$
 - (e) all values of x between $x = 2$ and $x = 5$, including $x = 5$ but not $x = 2$

3. The numerical values denoted by the inequality $1 < x \leq 2$ consist of:
 - (a) all values of x between $x = 1$ and $x = 2$, including $x = 1$ but not $x = 2$
 - (b) all values of x between $x = 1$ and $x = 2$, including $x = 2$ but not $x = 1$
 - (c) all values of x between $x = 1$ and $x = 2$, including neither $x = 1$ nor $x = 2$
 - (d) all values of x between $x = 1$ and $x = 2$, including both $x = 1$ and $x = 2$
 - (e) all values of x that are less than $x = 1$ as well as all values of x that are greater than $x = 2$, including $x = 2$.

4. The values of x that satisfy the inequality $1 + x > 2$ are:
- (a) all values of x between $x = 1$ and $x = 2$, not including either $x = 1$ or $x = 2$
 - (b) all values of x greater than $x = 1$, including $x = 1$
 - (c) all values of x less than $x = 1$, not including $x = 1$
 - (d) all values of x less than $x = 1$, including $x = 1$
 - (e) all values of x greater than $x = 1$, not including $x = 1$
5. The values of x that satisfy the inequality $2x < 3 + x$ are:
- (a) all values of x less than $x = 3$, not including $x = 3$
 - (b) all values of x between $x = 2$ and $x = 3$, not including $x = 2$ or $x = 3$
 - (c) all values of x between $x = 2$ and $x = 3$, including $x = 2$ but not $x = 3$
 - (d) all values of x between $x = 2$ and $x = 3$, including $x = 3$ but not $x = 2$
 - (e) all values of x greater than $x = 2$, not including $x = 2$
6. The values of x that satisfy the inequality $x > 4 - x$ are:
- (a) all values of x greater than $x = 2$, not including $x = 2$
 - (b) all values of x between $x = 1$ and $x = 4$, not including either $x = 1$ or $x = 4$
 - (c) all values of x between $x = 1$ and $x = 4$, including both $x = 1$ and $x = 4$
 - (d) all values of x between $x = 1$ and $x = 4$, including $x = 1$ but not $x = 4$
 - (e) all values of x between $x = 1$ and $x = 4$, including $x = 4$ but not $x = 1$
7. The values of x that satisfy the inequality $2x < 16 + x$ are:
- (a) all values of x greater than $x = 8$ but less than $x = 16$, not including either $x = 8$ or $x = 16$
 - (b) all values of x less than $x = 16$, not including $x = 16$
 - (c) all values of x less than $x = 8$, not including $x = 8$
 - (d) all values of x less than $x = 16$, including $x = 16$
 - (e) all values of x less than $x = 8$, including $x = 8$

- 8.** The values of x that satisfy the inequality $x^2 < 1$ are:
- (a) all values of x less than 1, not including $x = 1$
 - (b) all values of x between $x = -1$ and $x = 1$, not including $x = -1$ or $x = 1$
 - (c) all values of x less than $x = -1$, not including $x = -1$
 - (d) all values of x less than $x = -1$ and greater than $x = 1$, not including either $x = -1$ or $x = 1$
 - (e) all possible values of x .
- 9.** The values of x that satisfy the inequality $x^2 > 9$ are:
- (a) all values of x greater than $x = -3$, not including $x = -3$
 - (b) all values of x greater than $x = 3$, not including $x = 3$
 - (c) all values of x less than $x = -3$ and all values of x greater than $x = 3$, not including either $x = -3$ or $x = 3$
 - (d) all values of x between $x = -3$ and $x = 3$, not including either $x = -3$ or $x = 3$
 - (e) all values of x less than $x = 3$, not including $x = 3$
- 10.** The values of x that satisfy the inequality $x^2 < 4$ are:
- (a) all values of x less than $x = 2$, not including $x = 2$
 - (b) all values of x greater than $x = 2$, not including $x = 2$
 - (c) all values of x greater than $x = -2$, not including $x = -2$
 - (d) all values of x between $x = -2$ and $x = 2$, not including either $x = -2$ or $x = 2$
 - (e) all values of x less than $x = -2$, not including $x = -2$
- 11.** The values of x that satisfy the inequality $x^2 > 0$ are:
- (a) all values of x greater than $x = 0$, not including $x = 0$
 - (b) all values of x less than $x = 0$, not including $x = 0$
 - (c) all values of x that are both less than and greater than $x = 0$
 - (d) $x = 0$ only
 - (e) all values of x except for $x = 0$

- 12.** The values of x that satisfy the inequality $\frac{1}{x^2} < 100$ are:
- (a) all values of x greater than $x = 10$, not including $x = 10$
 - (b) all values of x less than $x = -10$, not including $x = -10$
 - (c) all values of x between $x = -10$ and $x = 10$, not including $x = -10$ or $x = 10$
 - (d) all values of x greater than $x = 10$, not including $x = 10$, and all values of x less than -10 , not including $x = -10$
 - (e) all values of x between $x = -10$ and $x = 10$ including both $x = -10$ and $x = 10$
- 13.** The values of x that satisfy the inequality $\frac{1}{x} > 3$ are:
- (a) all values of x greater than $x = 0$ and less than $x = 3$.
 - (b) all values of x between $x = -1/3$ and $x = 1/3$.
 - (c) all values of x greater than $x = 0$ and less than $x = 1/3$.
 - (d) all values of x greater than $x = 1/3$.
 - (e) There are no values of x that satisfy this inequality.
- 14.** The values of x that satisfy the inequality $4 < \frac{1}{x}$ are:
- (a) all values of x greater than $x = 4$.
 - (b) all values of x between $x = 0$ and $x = 0.25$.
 - (c) all values of x between $x = -0.25$ and $x = 0.25$.
 - (d) all values of x less than $x = -4$ and all values of x greater than $x = 4$.
 - (e) There are no values of x that satisfy this inequality.

15. The values of x that satisfy the inequality $\frac{1}{x+1} < \frac{1}{2}$ are:

- (a) all values of x greater than $x = 1$.
- (b) all values of x greater than $x = 0.5$.
- (c) all values of x between $x = -1$ and $x = 1$.
- (d) all values of x less than $x = -1$ and all values of x greater than $x = 1$.
- (e) There are no values of x that satisfy this inequality.

Answers:

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| 1. | C | 2. | D | 3. | B | 4. | E | 5. | A | 6. | A |
| 7. | B | 8. | B | 9. | C | 10. | D | 11. | E | 12. | D |
| 13. | C | 14. | B | 15. | A | | | | | | |