

## Problems for Gateway #1: Laws of Exponents

1. If  $x$  is a positive quantity, the expression  $\sqrt{\frac{x^{10}}{x^8}}$  could be simplified to:
- (a)  $x^{-2}$  (b)  $x^2$   
(c)  $x^{18}$  (d)  $x^9$   
(e)  $x$
2. The expression  $(a^2)^3$  could be simplified to:
- (a)  $a^6$  (b)  $a^5$   
(c)  $a^{2/3}$  (d)  $a^{3/2}$   
(e)  $a^{-1}$
3. If  $b$  is a positive quantity, the expression  $\frac{b}{\sqrt{b}}$  could be simplified to:
- (a)  $b^2$  (b)  $b^{1/2}$   
(c)  $b$  (d)  $b^{3/2}$   
(e) This expression cannot be simplified any further.
4. The expression  $\sqrt[3]{u^{18}}$  could be simplified to:
- (a)  $u^9$  (b)  $u^{54}$   
(c)  $u^{27}$  (d)  $u^6$   
(e)  $u^{15}$
5. The expression  $\frac{3}{x^2}$  could be simplified to:
- (a)  $3 + x^2$  (b)  $(3 \cdot x)^{-2}$   
(c)  $3 \cdot x^{-2}$  (d) 9  
(e)  $\left(\frac{3}{x}\right)^2$

6. The expression  $\frac{w^{10}}{w^9}$  could be simplified to:
- (a)  $w^{10/9}$  (b)  $w^{19}$   
(c)  $10 \cdot w^9$  (d)  $w^{-1}$   
(e)  $w$
7. The expression  $\left(\frac{a^2}{b}\right)^4$  could be simplified to:
- (a)  $\frac{a^2}{b^4}$  (b)  $\frac{a^6}{b}$   
(c)  $\frac{a^8}{b}$  (d)  $\frac{a^6}{b^4}$   
(e)  $\frac{a^8}{b^4}$
8. The expression  $(a^2 \cdot b)^5$  could be simplified to:
- (a)  $a^{10} \cdot b^5$  (b)  $a^2 \cdot b^5$   
(c)  $a^7 \cdot b$  (d)  $a^7 \cdot b^5$   
(e)  $a^{10} \cdot b$
9. The expression  $x^{10} \cdot x^3$  could be simplified to:
- (a)  $x^{30}$  (b)  $x^{13}$   
(c)  $x^7$  (d)  $x^{10/3}$   
(e) The expression cannot be simplified any further.
10. The expression  $b^4 \cdot \frac{b^2}{b^{10}}$  could be simplified to:
- (a)  $b^{16}$  (b)  $b^{0.6}$   
(c)  $b^{-8}$  (d)  $b^{-4}$   
(e)  $b^{14}$

11. The expression  $a^0 \cdot \sqrt{a}$  could be simplified to:
- (a)  $a^{1/2}$  (b)  $a^2$   
(c)  $a$  (d)  $a^{-1/2}$   
(e) 0
12. The expression  $\frac{\sqrt[3]{b}}{a^0}$  could be simplified to:
- (a)  $\left(\frac{b}{a}\right)^{1/3}$  (b)  $\left(\frac{b}{a}\right)^3$   
(c)  $b^{1/3}$   
(d) More information on  $a$  and  $b$  is needed in order to simplify any further.  
(e) The expression cannot be simplified because it is undefined.
13. If  $x$  is a positive quantity, the expression  $\sqrt[4]{\frac{1}{x}}$  could be simplified to:
- (a)  $4 \cdot x^{-1/2}$  (b)  $x^{-4}$   
(c)  $4x$  (d)  $\frac{4}{x}$   
(e)  $x^{-1/4}$
14. The expression  $(\sqrt[3]{u})^9$  could be simplified to:
- (a)  $u^{1/3}$  (b)  $u^3$   
(c)  $u^{9/2}$  (d)  $3 \cdot u^{9/2}$   
(e)  $u^{27}$
15. The expression  $(a^{-4})^4$  could be simplified to:
- (a)  $a^0$  (b) 1  
(c)  $a^8$  (d)  $a^{-16}$   
(e)  $a^{-8}$

**Answers:**

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|------------|----------|------------|----------|------------|----------|------------|----------|------------|----------|------------|----------|
| <b>1.</b>  | <b>E</b> | <b>2.</b>  | <b>A</b> | <b>3.</b>  | <b>B</b> | <b>4.</b>  | <b>D</b> | <b>5.</b>  | <b>C</b> | <b>6.</b>  | <b>E</b> |
| <b>7.</b>  | <b>E</b> | <b>8.</b>  | <b>A</b> | <b>9.</b>  | <b>B</b> | <b>10.</b> | <b>D</b> | <b>11.</b> | <b>A</b> | <b>12.</b> | <b>C</b> |
| <b>13.</b> | <b>E</b> | <b>14.</b> | <b>B</b> | <b>15.</b> | <b>D</b> |            |          |            |          |            |          |