

Problem Set # 3

10/01/04

1.2, # 12, 15, 18

1.3, # 1

Section 1.2

Problem 12.

- (a) (i) $g(h-1)$
 (ii) $g(h) - 10$
 (iii) $\frac{h}{2}$
 (iv) $g(h+6)$
 (v) $f(2)$
 (vi) $f(4) - f(2)$

Problem 15.

- (a) $g(0) = \frac{\sqrt{0^2+4}}{2} = 1$
 (b) $g(2) = \frac{\sqrt{2^2+4}}{2} = \frac{\sqrt{8}}{2} = \frac{2\sqrt{2}}{2} = \sqrt{2}$
 (c) $g(\sqrt{5}) = \frac{\sqrt{(\sqrt{5})^2+4}}{2} = \frac{\sqrt{5+4}}{2} = \frac{3}{2}$
 (d) $g(\frac{1}{\sqrt{2}}) = \frac{\sqrt{\frac{1}{2}+4}}{2} = \frac{3}{2\sqrt{2}}$
 (e) $-g(3t) = -\frac{\sqrt{(3t)^2+4}}{2} = -\frac{\sqrt{9t^2+4}}{2}$
 (f) $g(\sqrt{t-4}) = \frac{\sqrt{(\sqrt{t-4})^2+4}}{2} = \frac{\sqrt{t-4+4}}{2} = \frac{\sqrt{t}}{2}$

Problem 18.

- (a) 3
 (b) 7
 (c) $P(2W) = 5 - 2 \cdot (2W) = 5 - 4W$
 (d) $P(2W+1) = 5 - 2(2W+1) = 5 - 4W - 2 = 3 - 4W$
 (e) $P(W^2) = 5 - 2W^2$
 (f) $[P(W)]^2 = (5 - 2W)^2 = 4W^2 - 20W + 25$
 (g) $P(W^2+1) = 5 - 2(W^2+1) = 5 - 2W^2 - 2 = 3 - 2W^2$

Section 1.3

Problem 1.

- (a) (a) Function. Domain: $[-4, 5]$. Range: $[-.2, .9]$.
 (b) Not a function.
 (c) Function. Domain: $(-3, 7]$. Range: $[0, 3]$.
 (d) Function. Domain: $\{-3, -2, -1, 0, 1, 2, 3, 4\}$. Range: $\{-1, 0, 1\}$.
 (e) Not a function.
 (f) Function. Domain: $\{0, 1, 2, 3, 4\}$. Range: $\{1\}$.
 (g) Function. Domain: $(-\infty, \infty)$. Range: $[0, \infty)$.
 (h) Function. Domain: $[-1, 3]$. Range: $\{-1, 0, 1, 2\}$.
 (i) Function. Domain: $[-2, 0) \cup (0, 2]$. Range: $(-\infty, \infty)$.
 (b) None of the functions above is 1-to-1.