

$$8. \text{ Given: } y = \frac{\ln x^{1/2}}{x^{1/2}} = \frac{1}{2} \ln x \cdot x^{-1/2}$$

$$y' = \frac{1}{2} \left[ \ln x \cdot -\frac{1}{2} x^{-3/2} + \frac{1}{x} x^{-1/2} \right]$$

$$y' = \frac{1}{2} \left[ -\frac{\ln x}{2x^{3/2}} + \frac{1}{x^{3/2}} \right] = \frac{1}{4x^{3/2}} [-\ln x + 2]$$

$$9. W = W_0 \left[ 1 + \frac{r}{n} \right]^{15}$$

$$\frac{W}{W_0} = \left[ 1 + \frac{r}{n} \right]^{15}$$

$$\left( \frac{W}{W_0} \right)^{1/15} = 1 + \frac{r}{n}$$

$$\frac{r}{n} = \left( \frac{W}{W_0} \right)^{1/15} - 1$$

$$r = n \left( \frac{W}{W_0} \right)^{1/15} - n$$

$$10. \ln W = \ln W_0 + nt \ln \left( 1 + \frac{r}{n} \right)$$

$$\ln W - \ln W_0 = nt \ln \left( 1 + \frac{r}{n} \right)$$

$$\frac{\ln W - \ln W_0}{n \ln \left( 1 + \frac{r}{n} \right)} = t$$

$$11. e^t \frac{dy}{dt} + e^t + 2e^t = \frac{dy}{dt} - 2$$

$$e^t \frac{dy}{dt} - \frac{dy}{dt} = -3e^t - 2$$

$$\frac{dy}{dt} (e^t - 1) = -3e^t - 2$$

$$\frac{dy}{dt} = \frac{-3e^t - 2}{e^t - 1}$$

$$12. 3AB^{2x+1} = 5B$$

$$\frac{B^{2x+1}}{B} = \frac{5}{3A}$$

$$B^{2x} = \frac{5}{3A}$$

$$2x \ln B = \ln \left( \frac{5}{3A} \right)$$

$$x = \frac{\ln \left( \frac{5}{3A} \right)}{2 \ln B}$$

$$\text{or } \ln 3 + \ln A + (2x+1) \ln B = \ln 5B$$

$$(2x+1) \ln B = \ln 5B - \ln 3 - \ln A$$

$$2x+1 = \frac{\ln 5B - \ln 3A}{\ln B}$$

$$2x = \frac{\ln 5B - \ln 3A}{\ln B} - 1$$

$$x = \frac{1}{2} \left[ \frac{\ln 5B - \ln 3A}{\ln B} - 1 \right]$$

↔  
these are  
equivalent

$$13. B^2 + BC^t = 7BD$$

$$BC^t = 7BD - B^2$$

$$C^t = 7D - B$$

$$t \ln C = \ln (7D - B)$$

$$t = \frac{\ln (7D - B)}{\ln C}$$