

$$g) \ln(xy) = xy^2$$

$$\ln x + \ln y = xy^2 \quad (\text{this makes it easier})$$

$$\frac{d}{dx}(\ln x + \ln y) = \frac{d}{dx}(xy^2)$$

$$\frac{1}{x} + \frac{1}{y} \frac{dy}{dx} = x(2y) \frac{dy}{dx} + y^2$$

$$\frac{1}{x} - y^2 = 2xy \frac{dy}{dx} - \frac{1}{y} \frac{dy}{dx}$$

$$\frac{1}{x} - y^2 = \frac{dy}{dx} \left(2xy - \frac{1}{y} \right)$$

$$\frac{\frac{1}{x} - y^2}{2xy - \frac{1}{y}} = \frac{dy}{dx} \quad \text{or (simplified)} \quad \frac{dy}{dx} = \frac{y(y^2x - 1)}{x(1 - 2xy^2)}$$

17.4
#1

We know: $A = \pi r^2$ (for circle)

speed of Area increase = $\frac{dA}{dt}$

$$\frac{dA}{dt} = \pi(2r) \frac{dr}{dt} \quad (\text{remember chain rule})$$

$$\frac{dr}{dt} = 3 \frac{\text{ft}}{\text{sec}} \quad \text{radius} = 2 \text{ ft}$$

$$\frac{dA}{dt} = \pi(2 \cdot 2) \left(3 \frac{\text{ft}}{\text{sec}} \right) = 12\pi \frac{\text{ft}^2}{\text{sec}}$$