

15.1

#11

a) formula for continuous compounding

$$M = M_0 e^{rt}$$

$$M = (\$6000) e^{(0.05)t}$$

$$M = 6000 e^{(0.05)(7)} = \$8514.41$$

b) $t = t$

$$M = 6000 e^{0.05t}$$

$$c) M = M_0 e^{rt}$$

$$\frac{d}{dt} M = \frac{d}{dt} (M_0 e^{rt})$$

M_0 is constant!

$$\frac{dM}{dt} = M_0 e^{rt} \left(\frac{d}{dt} rt \right)$$

$$= M_0 e^{rt} (r) = (0.05)(6000) e^{0.05t}$$

$$= 300 e^{0.05t}$$

d) True!

$$M = 6000 e^{0.05t}$$

$$0.05M = (0.05) 6000 e^{0.05t}$$

$$= (0.05 \times 6000) e^{0.05t}$$

$$= 300 e^{0.05t} = \frac{dM}{dt}$$

✓

$$e) M = 6000 e^{0.05t} = 6000 \times (e^{0.05})^t$$

$$= 6000 \times (1.051)^t$$

$$= c a^t$$