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ii) $L(t)$ is increasing at a decreasing rate

$$\text{iii) } \frac{dL}{dt} = kL$$

$k > 0$ because the temperature $L(t)$ is still increasing.

iv) the difference in temperatures is described by

$$\frac{dD}{dt} = kD, \text{ so } D(t) = Ce^{kt}$$

@ $t=0$, difference = 25°

$$D(0) = 25 = Ce^{0t} \Rightarrow C = 25$$

$$\begin{aligned} L(t) &= 65 - (\text{difference in temps}) \\ &= 65 - 25e^{kt} \end{aligned}$$

@ $t=15$, temperature $L(15) = 50$

$$50 = 65 - 25e^{k(15)}$$

$$-15 = -25e^{15k}$$

$$\frac{3}{5} = e^{15k}$$

$$\ln \frac{3}{5} = 15k \Rightarrow k = -0.034$$

$$\therefore \boxed{L(t) = 65 - 25e^{-0.034t}}$$

$$\text{v) } L(t) = 55 = 65 - 25e^{-0.034t}$$

$$\boxed{t = 26.9 \text{ min}}$$