

**Homework Assignment 8: Due at the beginning of class 2/25/02**

Questions 1-5 of this assignment will always refer to the infinite series:

$$\sum_{k=1}^{\infty} \left( \frac{1}{k} - \frac{1}{k+1} \right).$$

1. Complete the entries in the table given below. One option here is to use a graphing calculator. For a reminder of the appropriate calculator commands to use, see the Appendix to this homework assignment.

Number of terms added	5	10	100	500	999
Total so far					

**NOTE:** You should hand in a completed table as part of your homework assignment.

2. Write out the sum that you need to evaluate to find the total of the first **ten** terms of the series, and simplify as much as possible.
3. Find an equation that gives the “total so far” (or “partial sum”) when the first  $N$  terms of the series are added together. (You can use the table from Question 1 to check the validity of your equation.) The only variable in your equation should be  $N$ .
4. By studying the limiting value of the “total so far” (or “partial sum”) it is possible to decide whether a series converges or diverges. In a paragraph, explain:
  - what it means for a series to “converge” or “diverge,” and,
  - how you can use the “total so far” (or “partial sum”) to decide whether a series converges or diverges.
5. Does the infinite series in this homework assignment converge or diverge? If you believe that the series converges, what value does it converge to?