

**Problems for Gateway #1: Convergence and Divergence of an  
Infinite Geometric Series**

1. The series that *CONVERGES* is:

(a)  $1 + \left(\frac{1}{2}\right) + \left(\frac{1}{2}\right)^2 + \left(\frac{1}{2}\right)^3 + \left(\frac{1}{2}\right)^4 + \dots$

(b)  $1 + (1.2)^2 + (1.2)^4 + (1.2)^6 + \dots$

(c)  $1 + (1.2) + (1.2)^2 + (1.2)^3 + \dots$

(d)  $1 + 2 + 2^2 + 2^3 + 2^4 + \dots$

2. The series that *CONVERGES* is:

(a)  $1 + (-3) + (-3)^2 + (-3)^3 + \dots$

(b)  $1 + 3 + 3^2 + 3^3 + 3^4 + \dots$

(c)  $1 + \left(\frac{-1}{3}\right) + \left(\frac{-1}{3}\right)^2 + \left(\frac{-1}{3}\right)^3 + \dots$

(d)  $1 + (-1) + (-1)^2 + (-1)^3 + (-1)^4 + \dots$

3. The series that *CONVERGES* is:

(a)  $\frac{1}{0.9} + \left(\frac{1}{0.9}\right)^2 + \left(\frac{1}{0.9}\right)^3 + \dots$

(b)  $0.9 + (0.9)^2 + (0.9)^3 + (0.9)^4 + \dots$

(c)  $1 + 9 + 9^2 + 9^3 + \dots$

(d)  $1.9 + (1.9)^2 + (1.9)^3 + (1.9)^4 + \dots$

4. The series that **DOES NOT CONVERGE** is:

- (a)  $9 + 9 \cdot \left(\frac{1}{2}\right) + 9 \cdot \left(\frac{1}{2}\right)^2 + 9 \cdot \left(\frac{1}{2}\right)^3 + \dots$
- (b)  $9 + 9 \cdot (0.9) + 9 \cdot (0.9)^2 + 9 \cdot (0.9)^3 + \dots$
- (c)  $1.1 + 1.1 \cdot (0.9) + 1.1 \cdot (0.9)^2 + 1.1 \cdot (0.9)^3 + \dots$
- (d)  $1 + 1.1 + (1.1)^2 + (1.1)^3 + \dots$

5. The series that **DOES NOT CONVERGE** is:

- (a)  $1 + (-0.1) + (-0.1)^2 + (-0.1)^3 + (-0.1)^4 + \dots$
- (b)  $1 + \left(\frac{2}{1.1}\right) + \left(\frac{2}{1.1}\right)^2 + \left(\frac{2}{1.1}\right)^3 + \left(\frac{2}{1.1}\right)^4 + \dots$
- (c)  $1 + \left(\frac{1}{1.1}\right) + \left(\frac{1}{1.1}\right)^2 + \left(\frac{1}{1.1}\right)^3 + \left(\frac{1}{1.1}\right)^4 + \dots$
- (d)  $1 + (0.1) + (0.1)^2 + (0.1)^3 + (0.1)^4 + \dots$

6. The series that **CONVERGES** is:

- (a)  $100 + 100 \cdot \left(\frac{1}{2}\right) + 100 \cdot \left(\frac{1}{2}\right)^2 + 100 \cdot \left(\frac{1}{2}\right)^3 + 100 \cdot \left(\frac{1}{2}\right)^4 + \dots$
- (b)  $0.001 + 0.001 \cdot (1.2)^2 + 0.001 \cdot (1.2)^4 + 0.001 \cdot (1.2)^6 + \dots$
- (c)  $0.0001 + 0.0001 \cdot (1.2) + 0.0001 \cdot (1.2)^2 + 0.0001 \cdot (1.2)^3 + \dots$
- (d)  $\frac{1}{10} + \frac{1}{10} + \frac{1}{10} + \frac{1}{10} + \frac{1}{10} + \dots$

7. The series that **CONVERGES** is:

- (a)  $1 + (1.3) + (1.3)^2 + (1.3)^3 + \dots$
- (b)  $10000 + 10000 \cdot (0.99) + 10000 \cdot (0.99)^2 + 10000 \cdot (0.99)^3 + \dots$
- (c)  $1.001 + (1.001)^2 + (1.001)^3 + (1.001)^4 + \dots$
- (d)  $1 + (-1) + (-1)^2 + (-1)^3 + (-1)^4 + \dots$

8. The series that **CONVERGES** is:

(a)  $\frac{1}{0.99} + \left(\frac{1}{0.99}\right)^2 + \left(\frac{1}{0.99}\right)^3 + \dots$

(b)  $9.9 + (9.9)^2 + (9.9)^3 + (9.9)^4 + \dots$

(c)  $1 + \frac{99}{100} + \left(\frac{99}{100}\right)^2 + \left(\frac{99}{100}\right)^3 + \dots$

(d)  $1.9 + (1.9)^2 + (1.9)^3 + (1.9)^4 + \dots$

9. The series that **DOES NOT CONVERGE** is:

(a)  $9 + 9 \cdot \left(\frac{1}{2}\right) + 9 \cdot \left(\frac{1}{2}\right)^2 + 9 \cdot \left(\frac{1}{2}\right)^3 + \dots$

(b)  $9 + 9 \cdot (0.9) + 9 \cdot (0.9)^2 + 9 \cdot (0.9)^3 + \dots$

(c)  $1.1 + 1.1 \cdot \left(\frac{1}{1.01}\right) + 1.1 \cdot \left(\frac{1}{1.01}\right)^2 + 1.1 \cdot \left(\frac{1}{1.01}\right)^3 + \dots$

(d)  $1 + \frac{1}{0.99} + \left(\frac{1}{0.99}\right)^2 + \left(\frac{1}{0.99}\right)^3 + \dots$

10. The series that **DOES NOT CONVERGE** is:

(a)  $1 + (-2.1) + (-2.1)^2 + (-2.1)^3 + (-2.1)^4 + \dots$

(b)  $1 + \left(\frac{2}{2.1}\right) + \left(\frac{2}{2.1}\right)^2 + \left(\frac{2}{2.1}\right)^3 + \left(\frac{2}{2.1}\right)^4 + \dots$

(c)  $1 + \left(\frac{1}{1.1}\right) + \left(\frac{1}{1.1}\right)^2 + \left(\frac{1}{1.1}\right)^3 + \left(\frac{1}{1.1}\right)^4 + \dots$

(d)  $1 + (0.1) + (0.1)^2 + (0.1)^3 + (0.1)^4 + \dots$

### Answers

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|----|---|----|---|----|---|-----|---|----|---|----|---|
| 1. | A | 2. | C | 3. | B | 4.  | D | 5. | B | 6. | A |
| 7. | B | 8. | C | 9. | D | 10. | A |    |   |    |   |