

Problems for Gateway #1: Distinguishing Finite and Infinite Series

1. Which of the following describes an infinite series?

- (a) $1 + 2 + 3 + 4 + 5$
- (b) $1 + 1.1 + 1.2 + 1.3 + 1.4 + \dots + 2$
- (c) $1 + 1.2 + 1.3 + 1.4 + \dots$
- (d) $1 + \frac{1}{1.1} + \frac{1}{1.2} + \frac{1}{1.3} + \dots + \frac{1}{2}$

2. Which of the following describes an infinite series?

- (a) $9 - 8 - 7 - 6 - \dots - 2 - 1$
- (b) $9 + 81 - 243 + \dots$
- (c) $9 + 9.9 + 9.99 + 9.999 + \dots + 9.99999999$
- (d) $9 + 90 + 900 + 9000 + 9 \times 10^{1000000}$

3. Which of the following describes an infinite series?

- (a) $1 + 1 + 1 + 1 + \dots$
- (b) $1 - 1 + 1 - 1 + 1 - \dots + (-1)^{34}$
- (c) $1 - 1 - 1 - 1 - 1$
- (d) $1 + 1 + 1 + 1 + 1$

4. Which of the following describes a finite series?

(a) $1 + 2 + 3 + 4 + \dots$

(b) $1 + \frac{1}{2} + \frac{1}{3} + \frac{1}{4} + \dots$

(c) $1 + \left(\frac{1}{2}\right)^2 + \left(\frac{1}{3}\right)^2 + \left(\frac{1}{4}\right)^2 + \dots$

(d) $1 + \left(\frac{1}{2}\right)^3 + \left(\frac{1}{3}\right)^3 + \left(\frac{1}{4}\right)^3 + \dots + \left(\frac{1}{100}\right)^3$

5. Which of the following describes a finite series?

(a) $1 - \frac{1}{2} + \frac{1}{4} - \frac{1}{8} + \dots - \left(\frac{1}{2}\right)^{17}$

(b) $1 + \frac{1}{2} + \frac{1}{4} - \frac{1}{8} - \frac{1}{16} + \frac{1}{32} + \frac{1}{64} - \dots$

(c) $1 - \frac{1}{2} + \frac{1}{4} - \frac{1}{8} + \dots$

(d) $1 + \frac{1}{2} + \frac{1}{4} + \frac{1}{8} + \dots$

6. Which of the following describes an infinite series?

(a) $1 + 2 + 3 + 4 + 5 + 6 + 7 + 8 + n + \dots$

(b) $0.0 - 1.1 - 2.2 - 3.3 - 4.4 - \dots - 20.20$

(c) $1 + 11 + 111 + 1111 + 11111 + \dots + 1111111111$

(d) $\frac{1}{1} + \frac{1}{2} + \frac{1}{3} + \dots + \frac{1}{n} + \dots + \frac{1}{2000}$

7. Which of the following describes an infinite series?

- (a) $1 + 2 + 4 + 8 + \dots + 2^n + \dots + 1024$
- (b) $1 + 6 + 66 + 666 + \dots$
- (c) $1 + 1.9 + 1.99 + 1.999 + \dots + 1.99999999$
- (d) $10 + 10^2 + 10^3 + \dots + 10^n + \dots + 10^{1000000}$

8. Which of the following describes an infinite series?

- (a) $1 + \frac{1}{2} + \frac{1}{4} + \frac{1}{8} + \dots + \frac{1}{2^n} + \dots + \frac{1}{256}$
- (b) $1 - 2 + 3 - 4 + 5 - \dots + (-1)^{n+1} \cdot n + \dots - 17$
- (c) $1 - 1 - 1 - 1 - 1 - 1 - \dots - 1^n - \dots - 1^{100}$
- (d) $1 - 2 + 3 - 4 + 5 - \dots + (-1)^{n+1} \cdot n + \dots$

9. Which of the following describes a finite series?

- (a) $1 + 2^2 + 3^3 + 4^4 + \dots$
- (b) $1 + \frac{1}{e} + \frac{1}{e^2} + \frac{1}{e^3} + \dots$
- (c) $1 + e + e^2 + \dots + e^n + \dots + e^{100}$
- (d) $1 + \left(\frac{1}{2}\right)^2 + \left(\frac{1}{3}\right)^3 + \left(\frac{1}{4}\right)^4 + \dots + \left(\frac{1}{n}\right)^n + \dots$

10. Which of the following describes a finite series?

- (a) $1 - 2 + 4 - 8 + \dots + (-1)^n \cdot 2^n + \dots - 2^{12}$
- (b) $1 + 2^{10} + 3^{10} + \dots + n^{10} + \dots$
- (c) $1 + \frac{1}{2^{10}} + \frac{1}{3^{10}} + \dots + \frac{1}{n^{10}} + \dots$
- (d) $1 + \frac{1}{4} + \frac{1}{9} + \frac{1}{16} + \dots + \frac{1}{n^2} + \dots$

Answers

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| 1. | C | 2. | B | 3. | A | 4. | D | 5. | A | 6. | A |
| 7. | B | 8. | D | 9. | C | 10. | A | | | | |