

18.5

$$- 4. \quad 32 + 32(.6) + 32(.6)^2 + \dots = \frac{32}{1-(.6)} = 80$$

$$11. \quad 4000 = P\left(1 + \frac{.045}{12}\right)^{23} + P(1.00375)^{22} + \dots \Rightarrow P = \frac{P(1 - (1.00375)^{24})}{1 - (1.00375)} = 25.06P \Rightarrow P = \$159.59$$

$$- 16.(a) \quad 100000 = \frac{P}{(1.01)^{360}} + \frac{P}{(1.01)^{359}} + \dots + \frac{P}{(1.01)^1} = \frac{P\left(\left(\frac{1}{1.01}\right)^1 - \left(\frac{1}{1.01}\right)^{361}\right)}{1 - \left(\frac{1}{1.01}\right)} \Rightarrow P \approx \$1028.61$$

$$(b) \quad 100000 = \frac{Q\left(\frac{1}{1 + \frac{.0675}{12}} - \left(\frac{1}{1 + \frac{.0675}{12}}\right)^{361}\right)}{1 - \left(\frac{1}{1 + \frac{.0675}{12}}\right)} \Rightarrow Q \approx 648.60, \text{ hence she has monthly savings of } \$380.01$$

19. Using the half-life, $1 = 2e^{3k} \Rightarrow \ln\left(\frac{1}{2}\right) = 3k \Rightarrow k = \frac{1}{3}\ln\left(\frac{1}{2}\right)$.

(a) $SAR = 2 + 2e^{3k} + 2e^{6k} + \dots = 2 + 1 + \frac{1}{2} + \frac{1}{4} + \dots = \frac{2}{1 - \frac{1}{2}} = 4$ is upper limit, never quite reached.

(b) $SAB = 2 + 2e^{2k} + 2e^{4k} + \dots = \frac{2}{1 - e^{2k}} \approx 5.4048$, so he eventually gets to a level above the equivalent of taking 5 all at once.