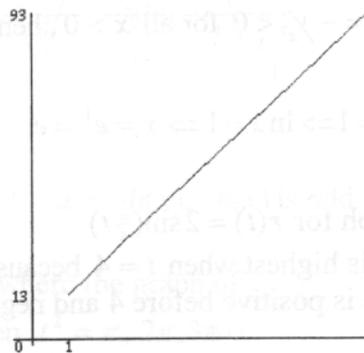


2. The region above interval $[1, 9]$ under the graph is a trapezoid, hence the area is $\frac{1}{2}(13 + 93)(9 - 1) = 424$.

This supports:

$$\int_1^9 (10t + 3) dt = (5t^2 + 3t) \Big|_1^9 = (405 + 27) - (5 + 3) = 424$$

5. $\int_0^1 e^x dx = (e^x) \Big|_0^1 = e^1 - e^0 = e - 1$.



6. (a) $\int_{-1}^0 e^{-x} dx = (-e^{-x}) \Big|_{-1}^0 = -e^0 - (-e^{-(-1)}) = -1 + e = e - 1$.

These regions are mirror images across the y-axis.

(b) $\int_0^1 e^{-x} dx = (-e^{-x}) \Big|_0^1 = -e^{-1} - (-e^0) = -\frac{1}{e} + 1 = 1 - \frac{1}{e}$.

8. (a) Rate of change is negative so it is cooling.

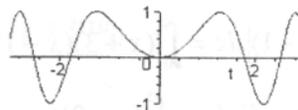
(b) $\int_0^1 -2e^{-t} dt = 2e^{-t} \Big|_0^1 = \frac{2}{e} - 2$ degrees.

(c) $\int_1^2 -2e^{-t} dt = 2e^{-t} \Big|_1^2 = \frac{2}{e^2} - \frac{2}{e}$ degrees.

(d) 100 plus change = $100 + \frac{2}{e} - 2 = 98 + \frac{2}{e}$ degrees.

- 13.(a) See graph of $y = \sin(t^2)$ to the right.

- (b) $h(x) > 0$ on $(0, \infty)$ as positive signed area always overpowers negative signed area.



(c) $h(-x) = \int_0^{-x} \sin(t^2) dt = -\int_{-x}^0 \sin(t^2) dt =$

$-(\text{area of the region reflected across the y-axis}) = -\int_0^x \sin(t^2) dt = -h(x)$, $h(x)$ is odd.

- (d) $h(x)$ changes from increasing to decreasing to increasing where the graph of $\sin(t^2)$ crosses the t -axis. That is when $\sin(t^2) = 0$, when $t^2 = \pi, 2\pi, 3\pi \dots$ increasing on $[0, \sqrt{\pi}]$, decreasing on $[\sqrt{\pi}, \sqrt{2\pi}]$ and increasing on $[\sqrt{2\pi}, 3]$.

- (e) Maximum = 1 and minimum = -1.

- (f) On $[0, 3]$ h has a global min. at 0, a global max. at $\sqrt{\pi}$ and a local min at $\sqrt{2\pi}$.

On $(0, \infty)$ 0 is no longer in the interval so we have no global minimum. We still have a global maximum at $\sqrt{\pi}$. There will be infinitely many more local maximum and minimum points. On $(-\infty, \infty)$ the global max is at $\sqrt{\pi}$ and the global min is at $-\sqrt{\pi}$.

(g) $h(\sqrt{\pi}) \cong 0.895$