

## ENTRY COMPUTABILITY

[ENTRY COMPUTABILITY] Authors: Oliver Knill: nothing real yet Literature: not yet, some lectures of E.Engeler on computation theory

### Church's theses

The generally accepted [Church's theses] tells that everything which is computable can be computed using a Turing machine. In that case, the problem to determine, whether a Turing machine will halt, is not computable.

### cipher

A [cipher] is a secret mode of writing, often the result of substituting numbers of letters and then carrying out arithmetic operations on the numbers.

### Coding theory

[Coding theory] is the theory of encryption of messages employed for security during the transmission of data or the recovery of information from corrupted data.

### Cooks hypothesis

[Cooks hypothesis]  $P = NP$ . A proof or disproof is one of the millenium problems.

### Graph isomorphism problem

[Graph isomorphism problem] It is not known whether graph isomorphism can be decided in deterministic polynomial time. It is an open problem in computational complexity theory.

### Inductive structure

[Inductive structure] A set  $U$  with a subset  $A$  and operations  $g_1, \dots, g_n$  define an inductive structure  $(U, A, g_1, \dots, g_n)$  if all elements of  $U$  can be generated by repeated applications of the operations  $g_i$  on elements of  $A$ . Examples:

- $(N, A = \{0, 1\}, g_1(a, b) = a + b, g_2(a, b) = a * b)$  defines an inductive structure.
- If  $U = N$  is the set of natural numbers,  $A = \{1, 2, 3\}$   $g_1(x, y) = 3x - 4, g_2(x, y, z) = 7x + 5y - z$ , then  $(U, A, g_1, g_2)$  define an inductive structure.

## syntactic structure

An inductive structure  $(U, A, g_1, \dots, g_n)$  is called a [syntactic structure] if it is uniquely readable that is if  $g_1(u_1, \dots, u_k) = g_2(v_1, \dots, v_l)$ , then  $g_1 = g_2, k = l$  and  $u_1 = v_1, \dots, u_k = v_k$ . Example: if  $X$  is the set of finite words in the alphabet  $\{p, q, r, K, N\}$  and  $A = \{p, q, r\}$ . Define  $g_1(x, y) = Kxy$  and  $g_2(x, y) = Nx$  and  $U$  the set of words generated from  $A$ . The structure is the language of elementary logic in polnic notation. It is a syntactic structure. Syntactic structures are in general described by grammars.

## grammar

A [grammar]  $(N, T, G)$  is given by two sets of symbols  $N, T$  and a finite set  $G$  of pairs  $(n_i, t_i)$  which define transitions  $n_i \rightarrow t_i$ . For example:  $N = \{S\}, T = \{K, N, p, q, r\}, G = \{S \rightarrow p, S \rightarrow q, S \rightarrow r, S \rightarrow KSS, S \rightarrow NS\}$ . According to Chomsky, one classifies grammars with additional conditions like context sensitivity or regularity.

## context sensitive

A grammar  $(N, T, G)$  is called [context sensitive] if  $(n, t) \in G$  then  $|t| \geq |n|$ .

## context sensitive

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