

# *LECTURE 2*

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# *PLAN*

1. Function Poll, Review

2. Function Zoo

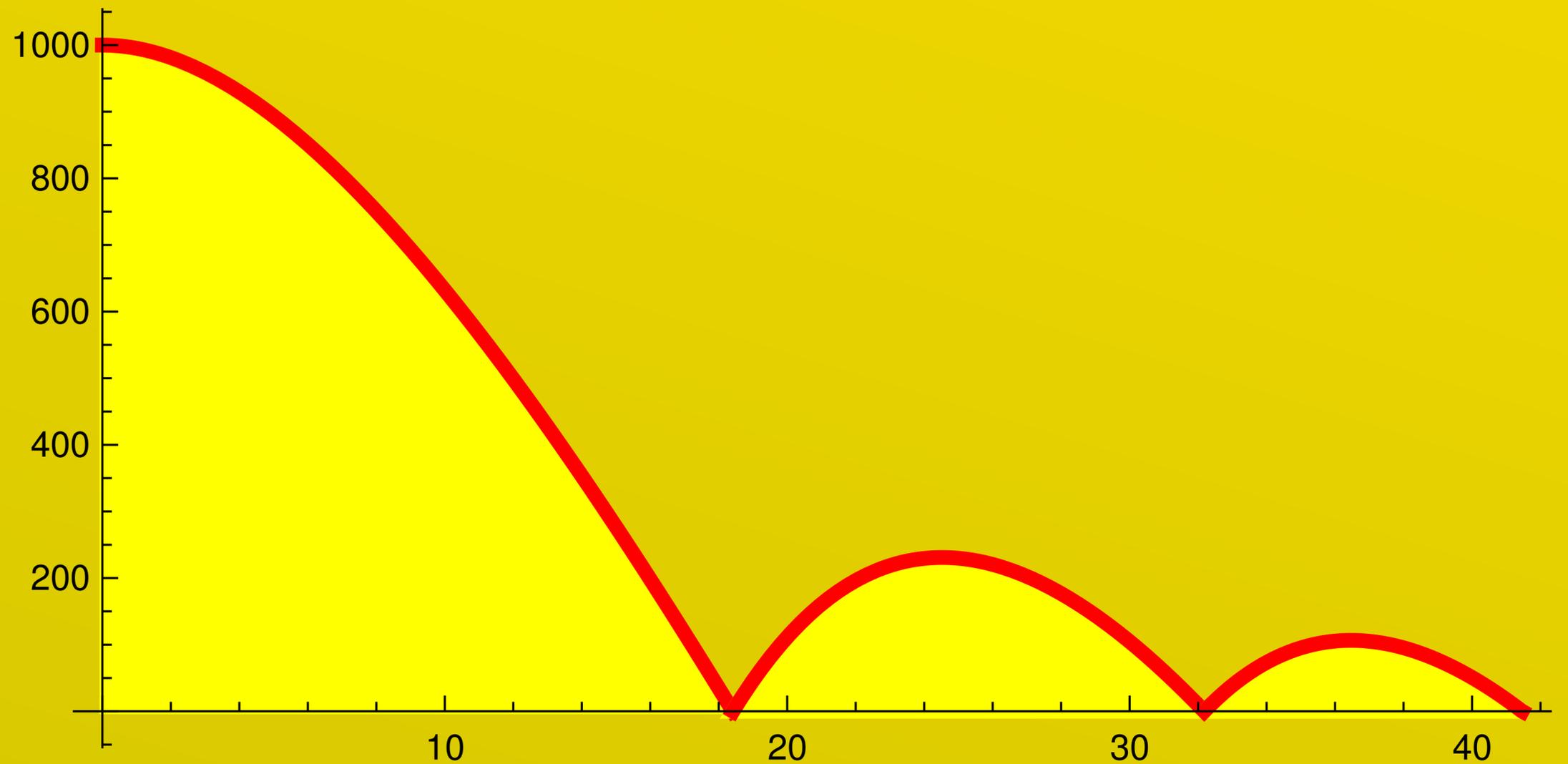
3. Plotting

4. Bungee jump

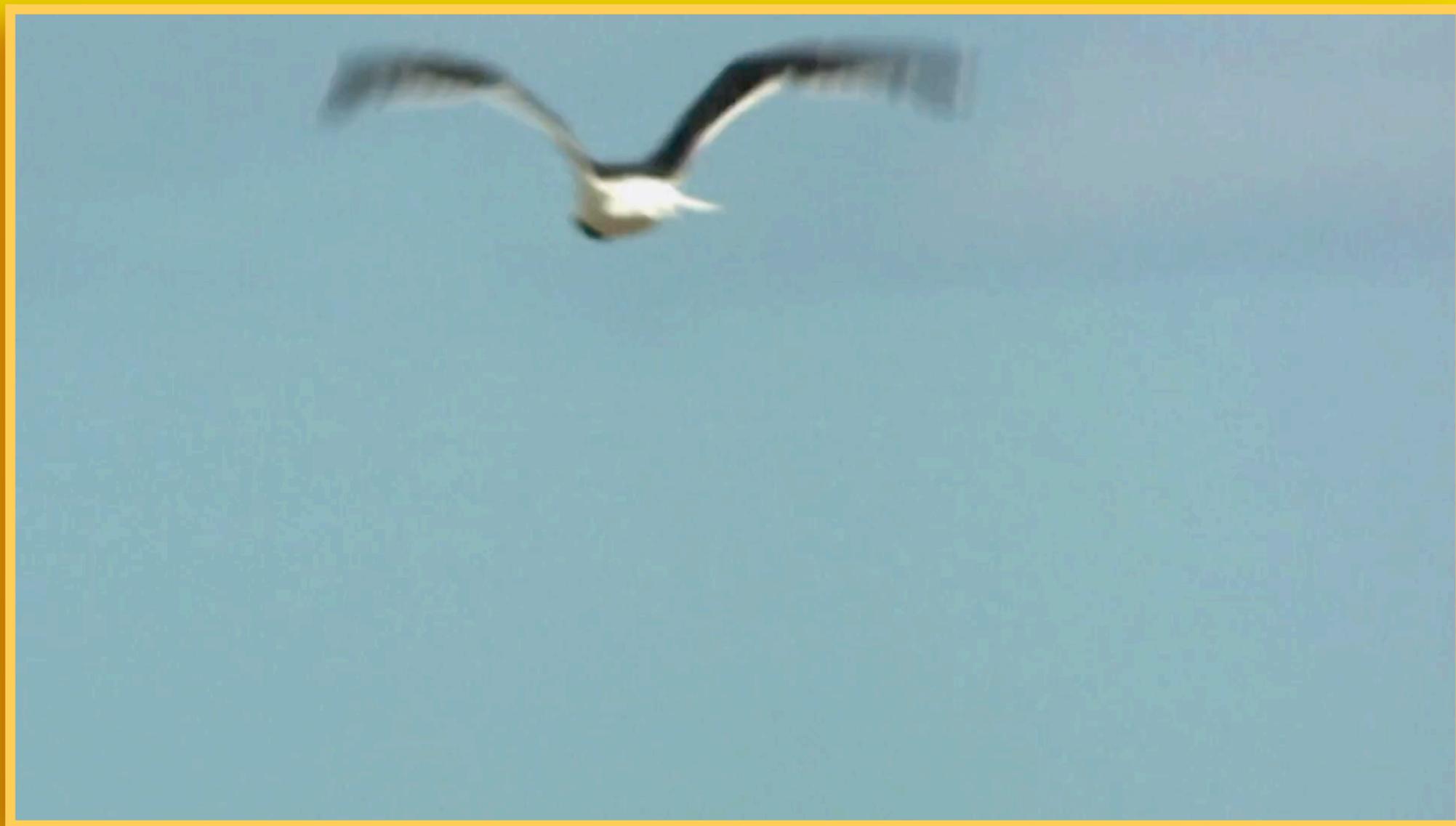
5. Daylight time

6. Tax System

# REVIEW BOUNCE



*DROPPING  
A SHELL*



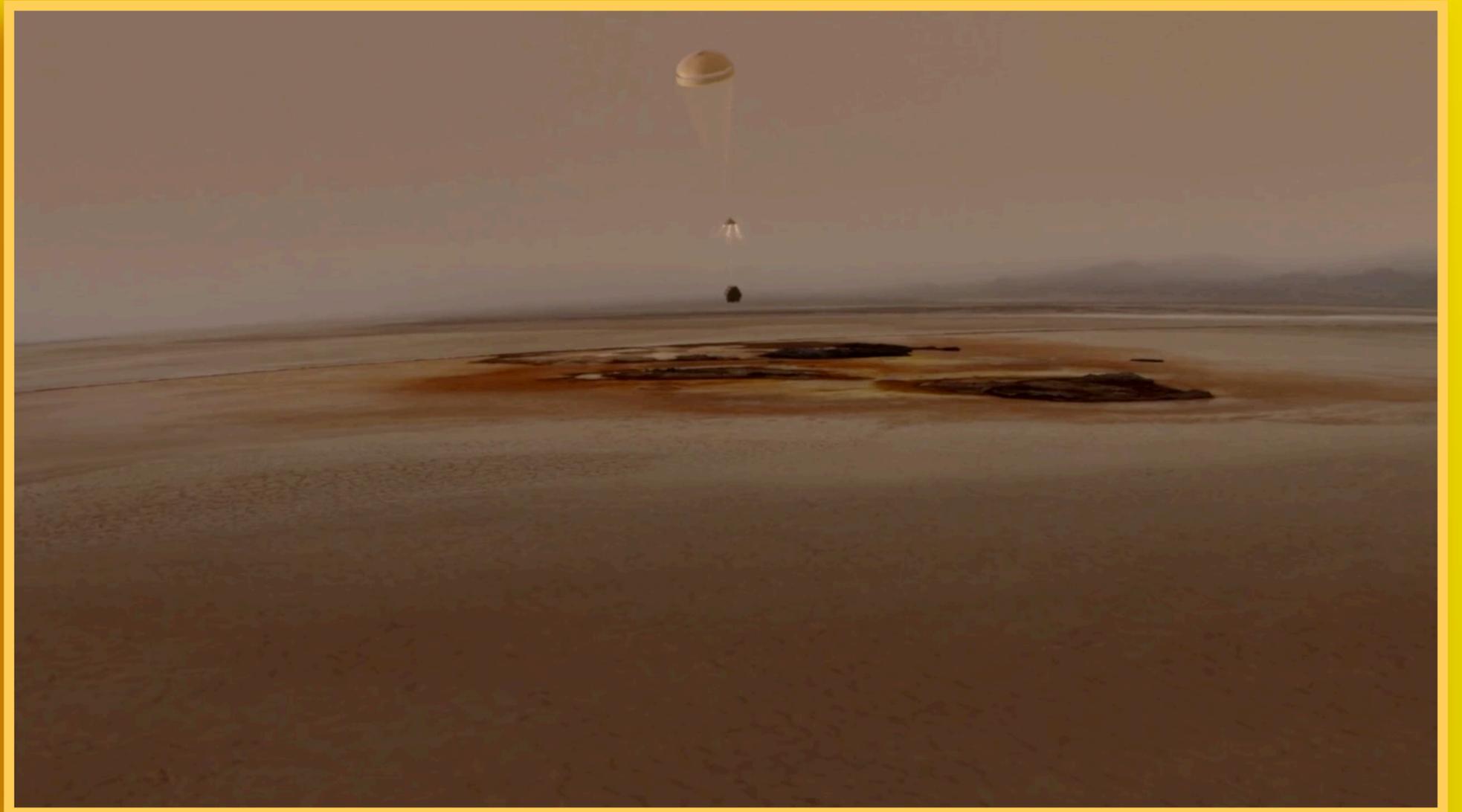
# *BOUNCING ON ASTEROID*



# *DAM BUSTERS*



# *MARS BOUNCE*

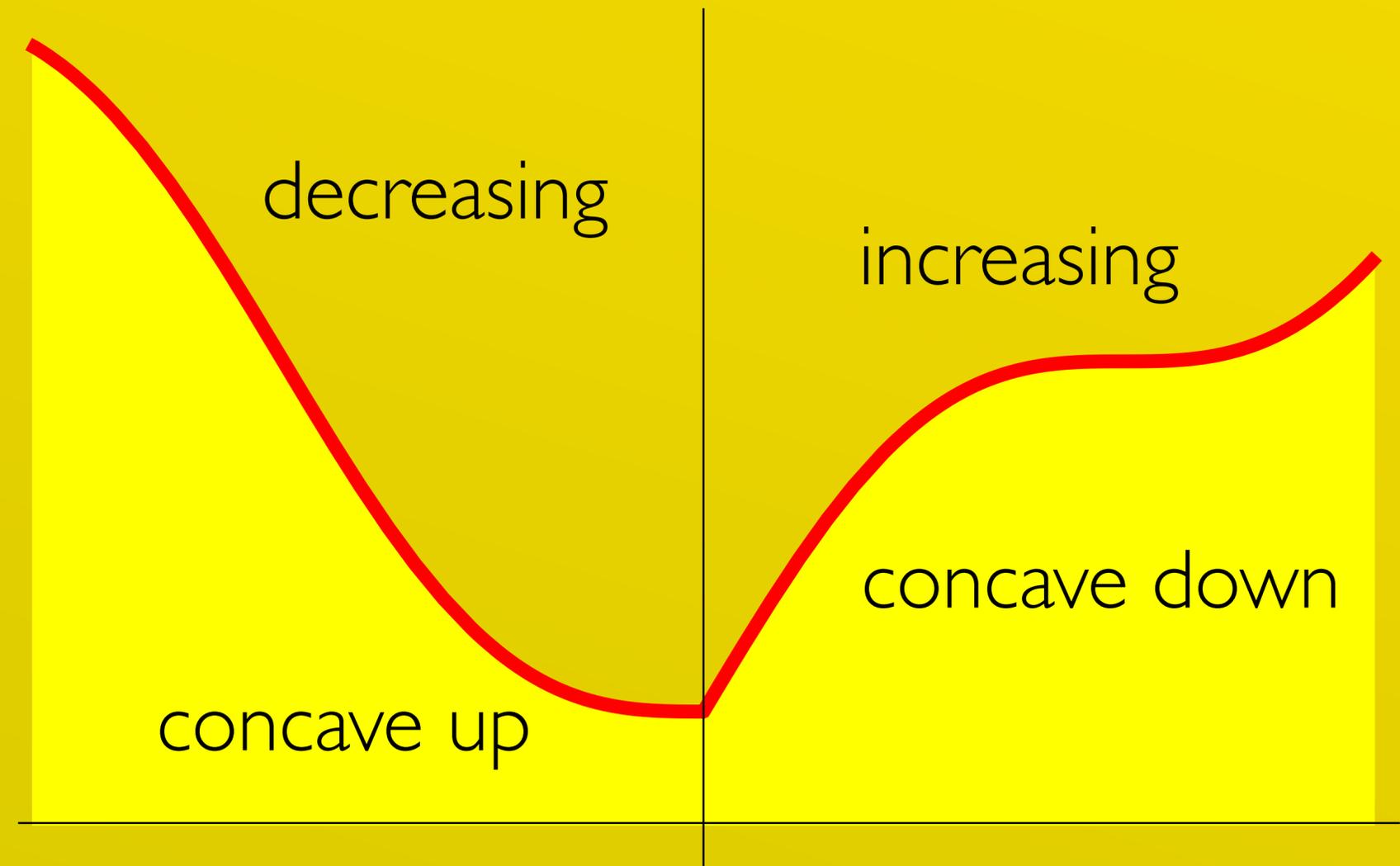


*FUNCTION ZOO*

*GROW THEM LIVE  
IN CLASS*

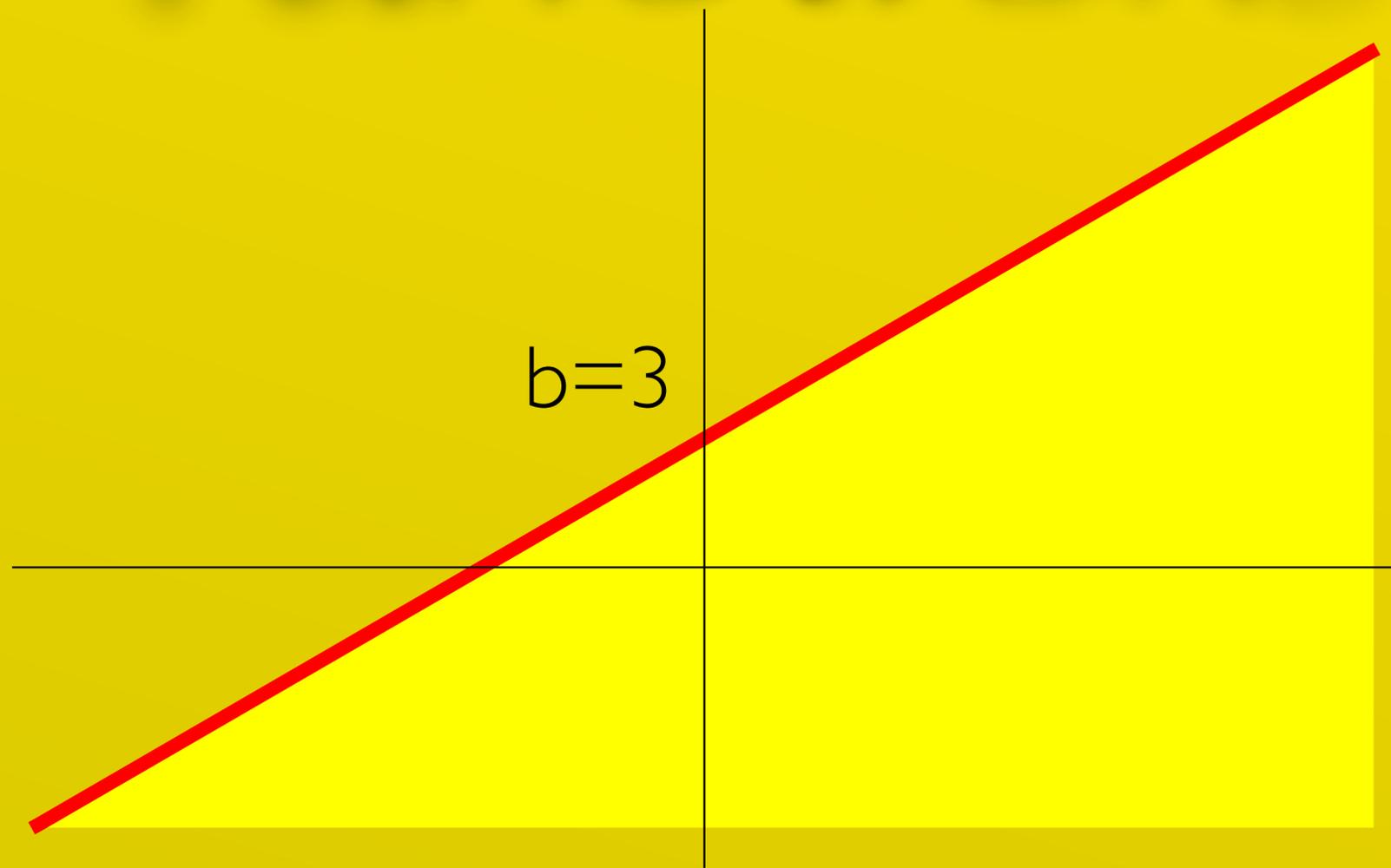
# FUNCTIONS

$$f(x) = |x| + \sin(x) + 1$$



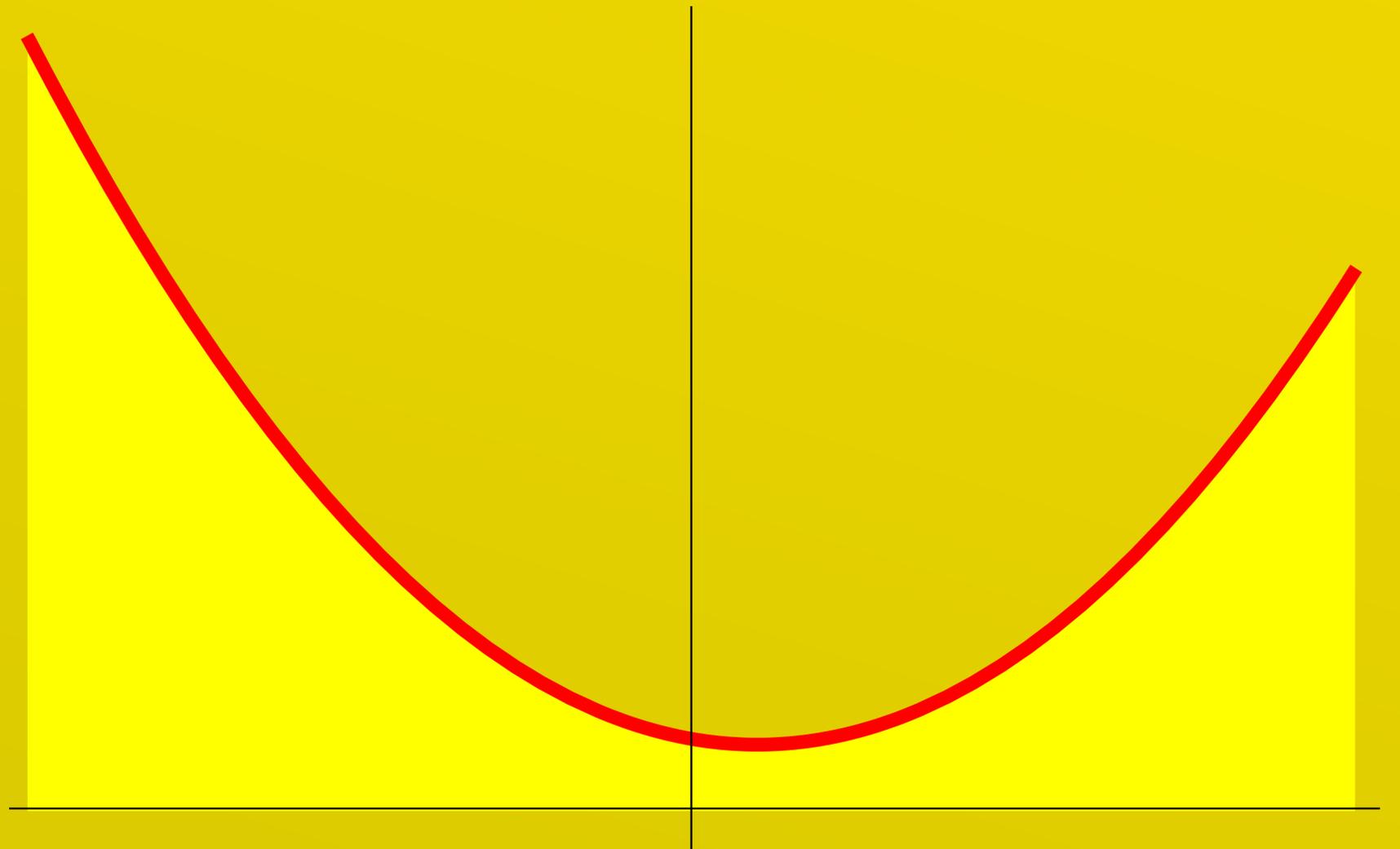
# *LINEAR FUNCTIONS*

$$f(x) = x + 3$$



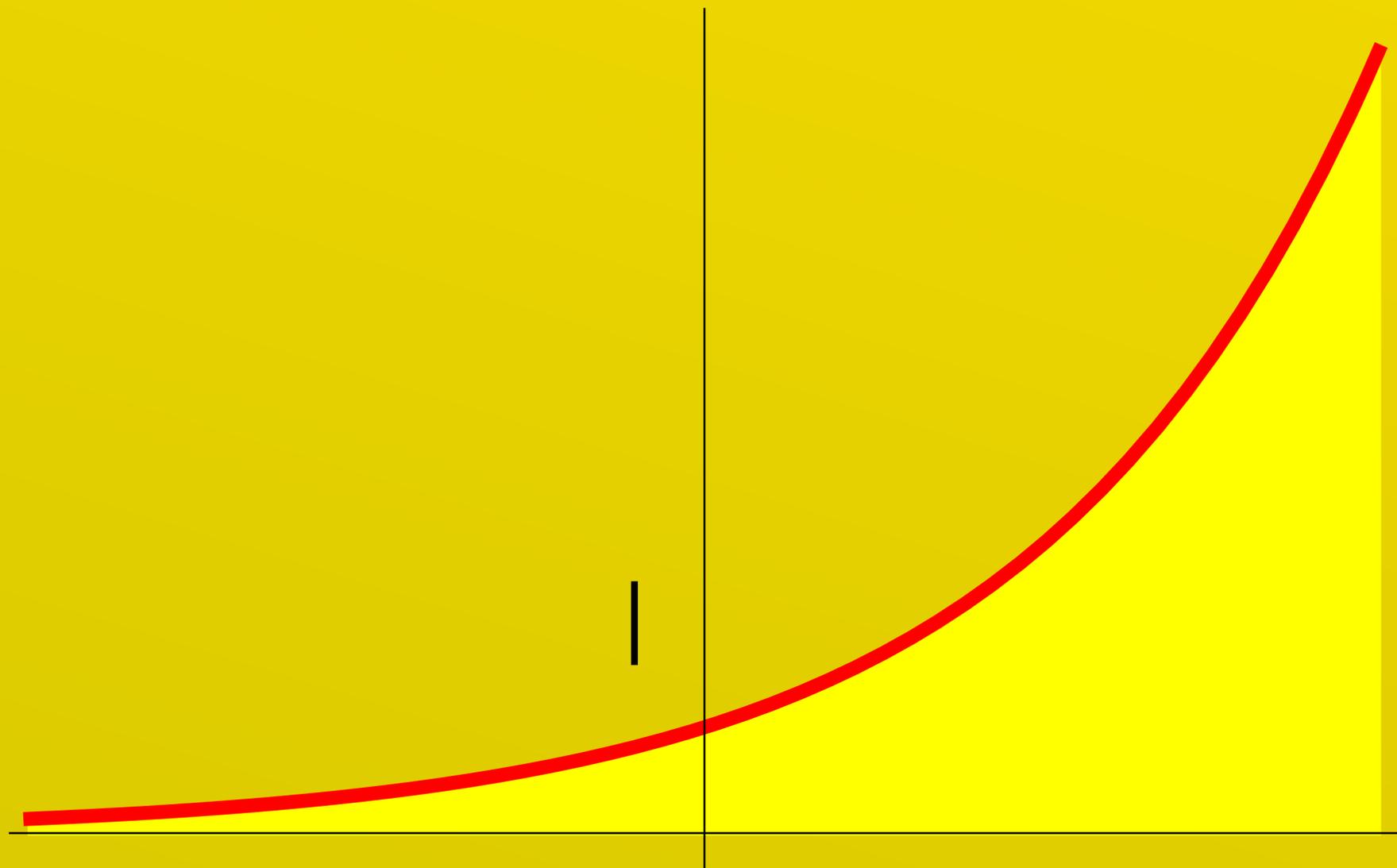
# POLYNOMIAL FUNCTIONS

$$f(x) = x^2 - x + 3$$



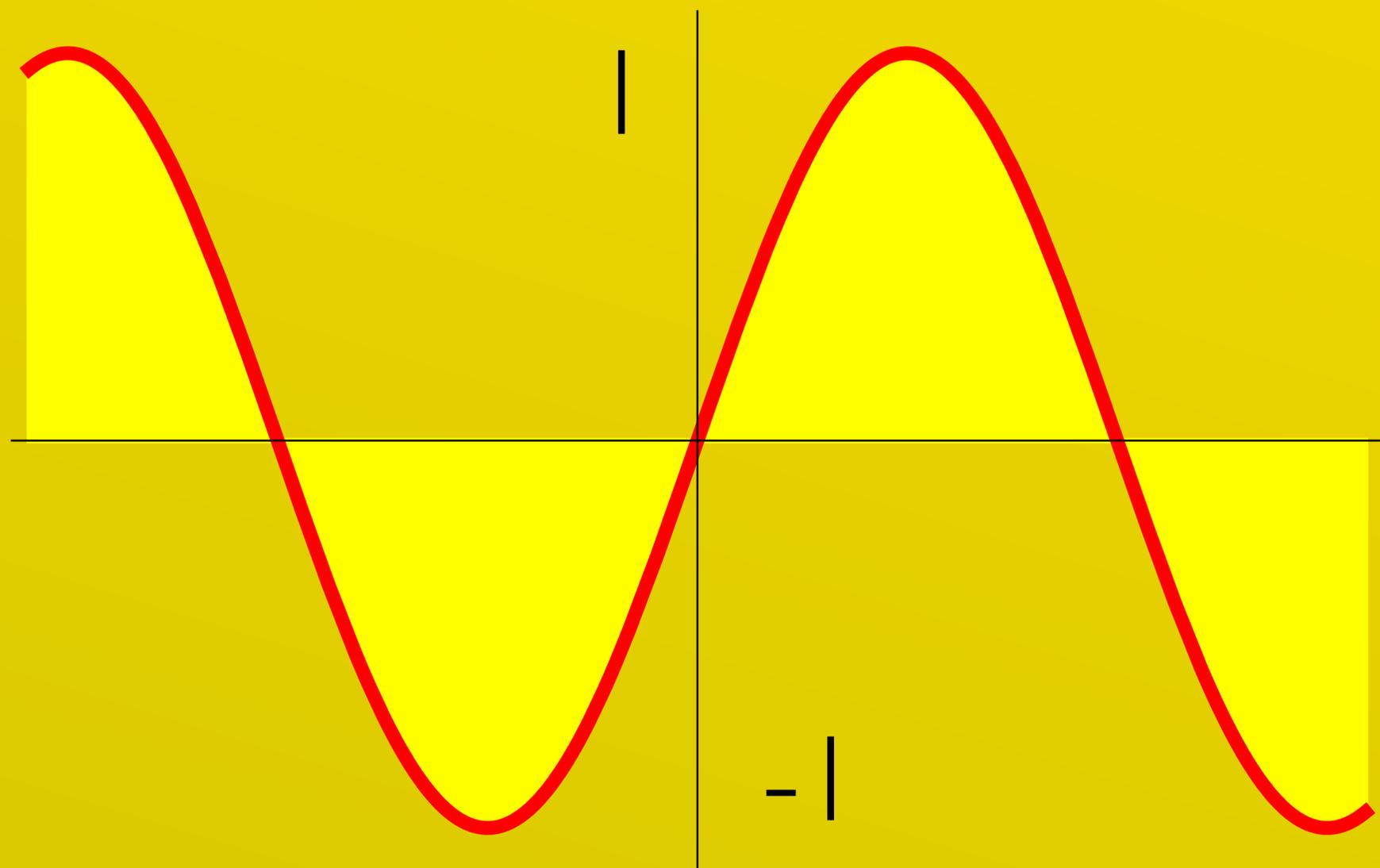
# EXPONENTIAL FUNCTIONS

$$f(x) = e^x = \exp(x)$$



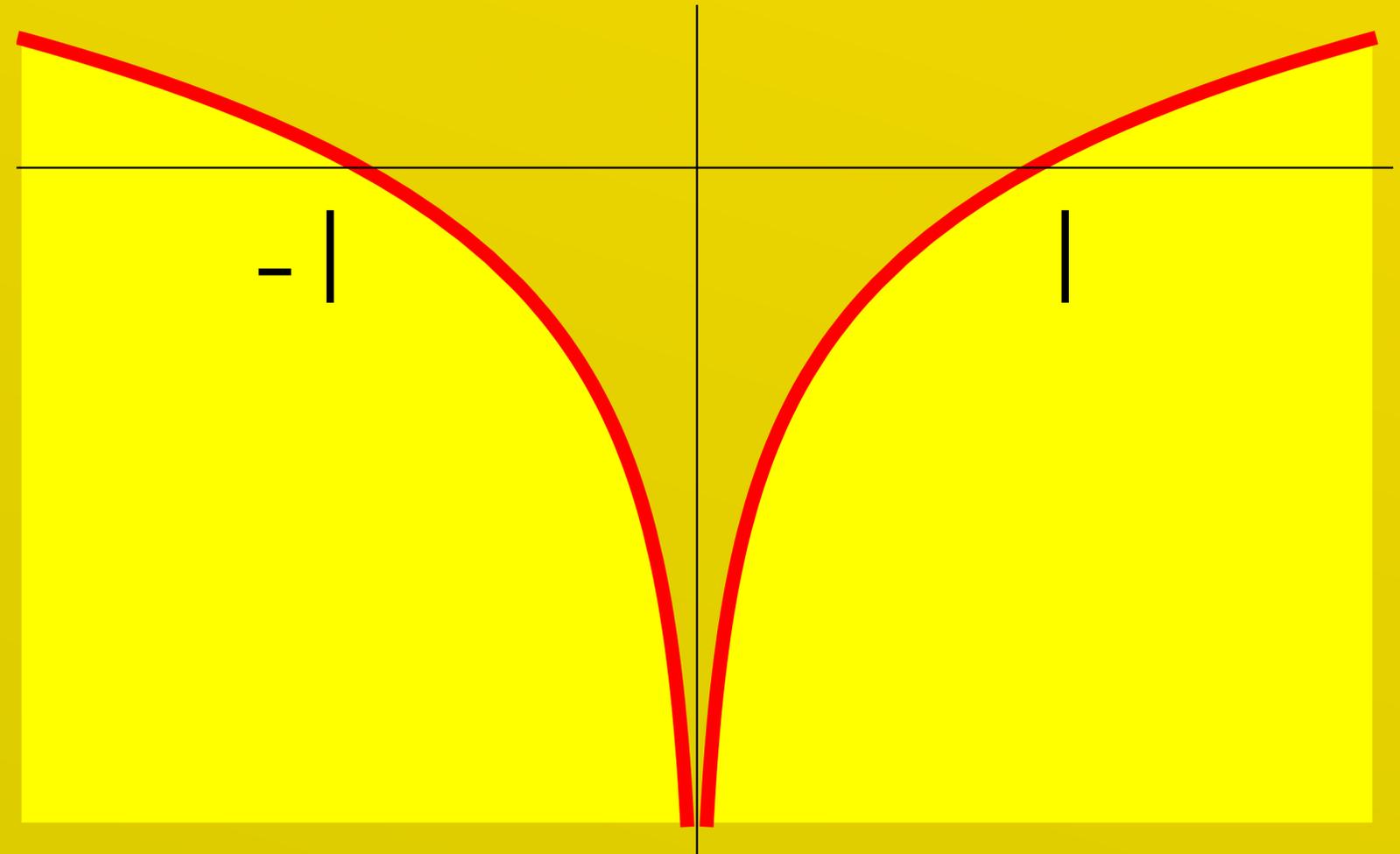
# TRIG FUNCTIONS

$$f(x) = \sin(x)$$



# LOG FUNCTION

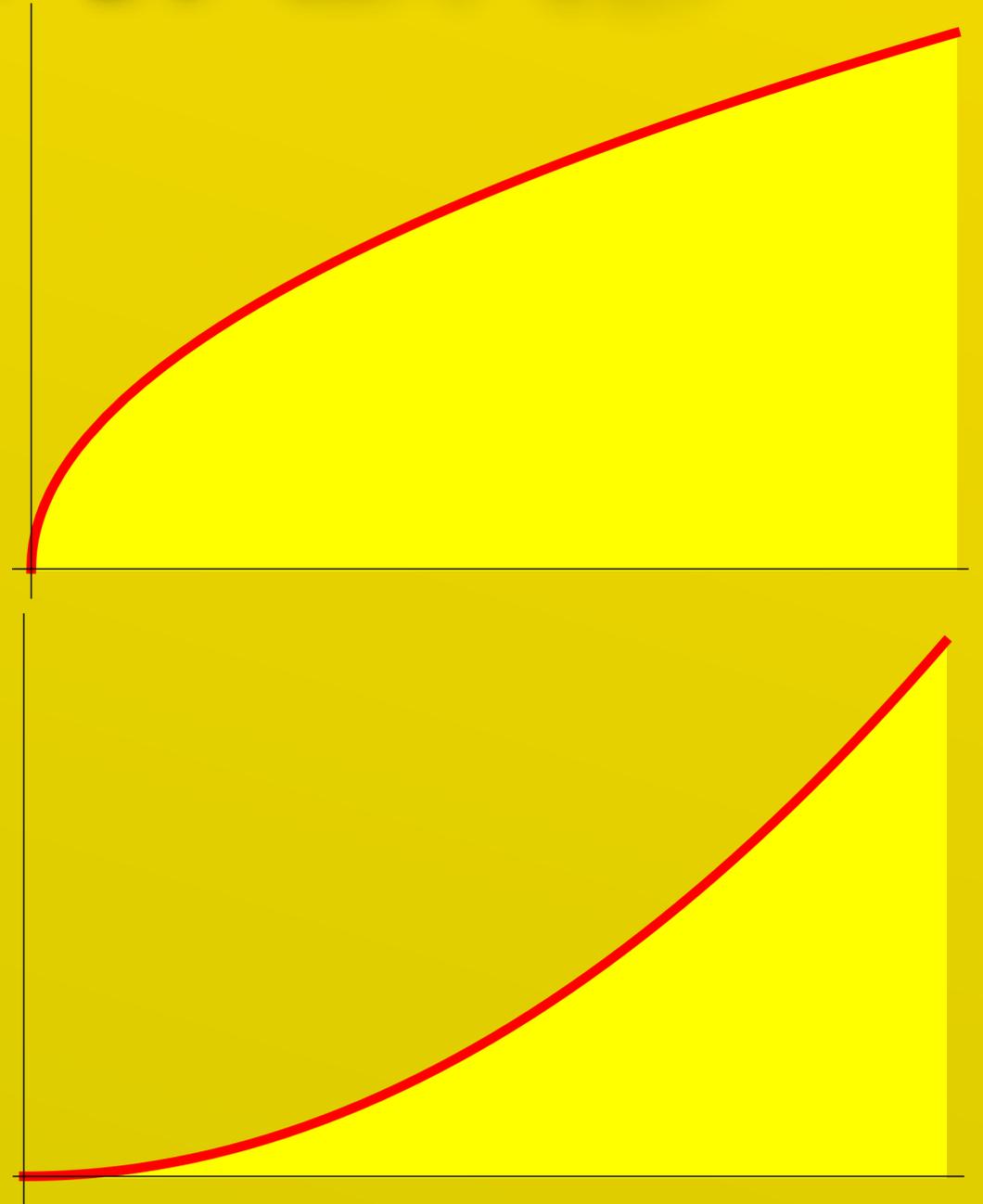
$$f(x) = \ln |x| = \log |x|$$



# *INVERSE FUNCTIONS*

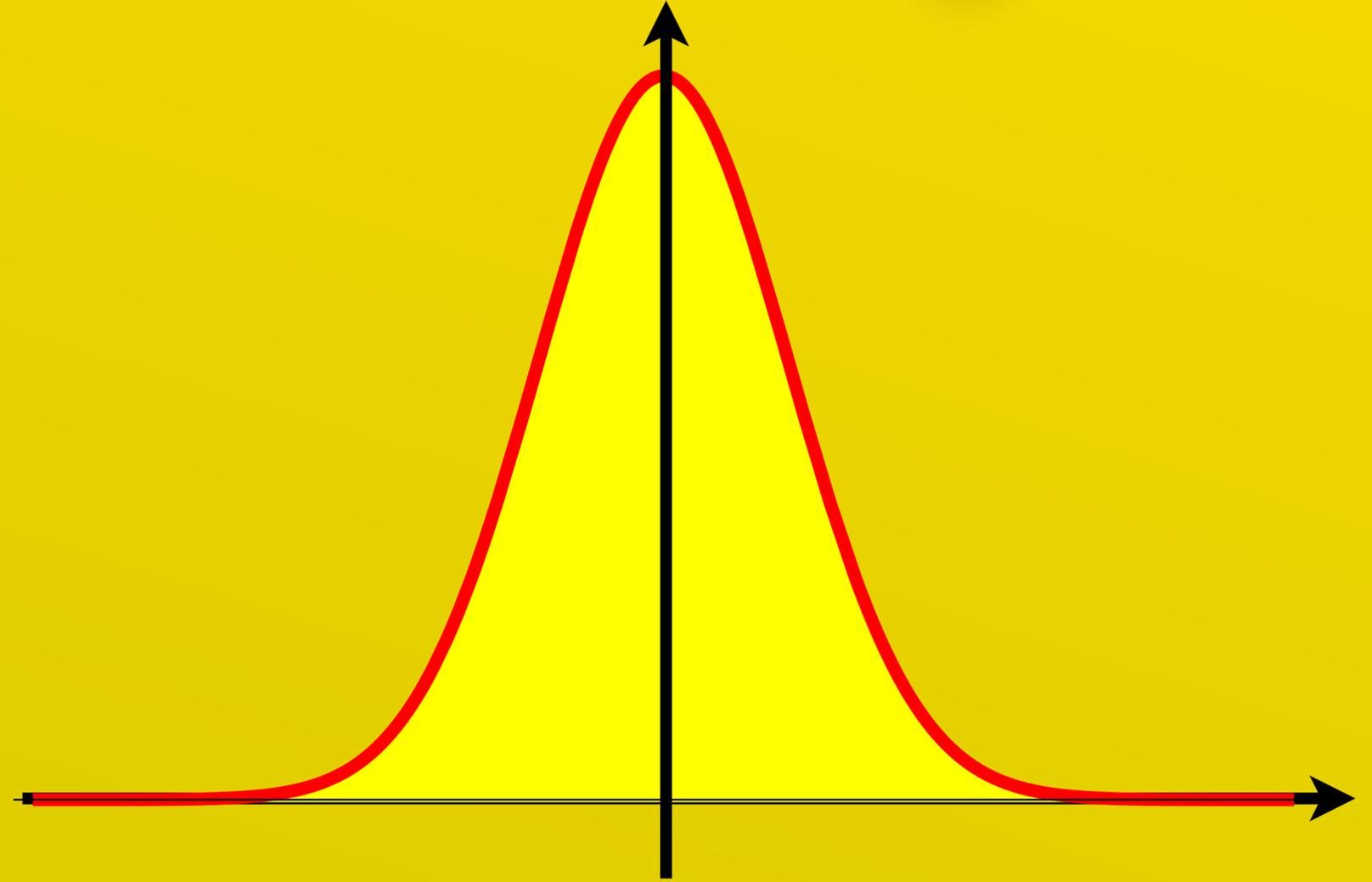
$$y = x^2$$

$$y = \sqrt{x}$$



# COMPOSING

$$f(x) = e^{-x^2}$$



BELL CURVE

# *Functions*

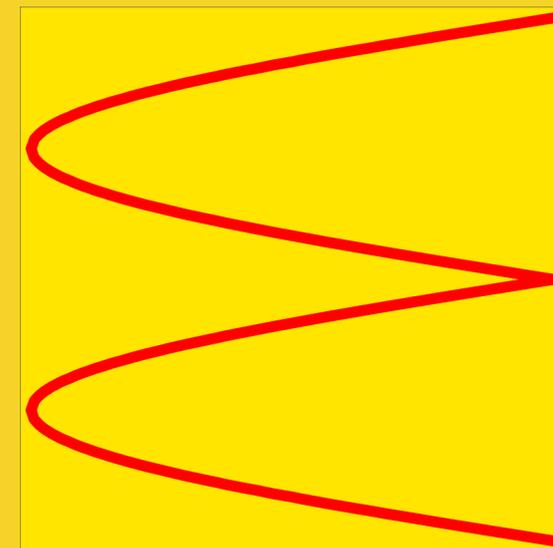
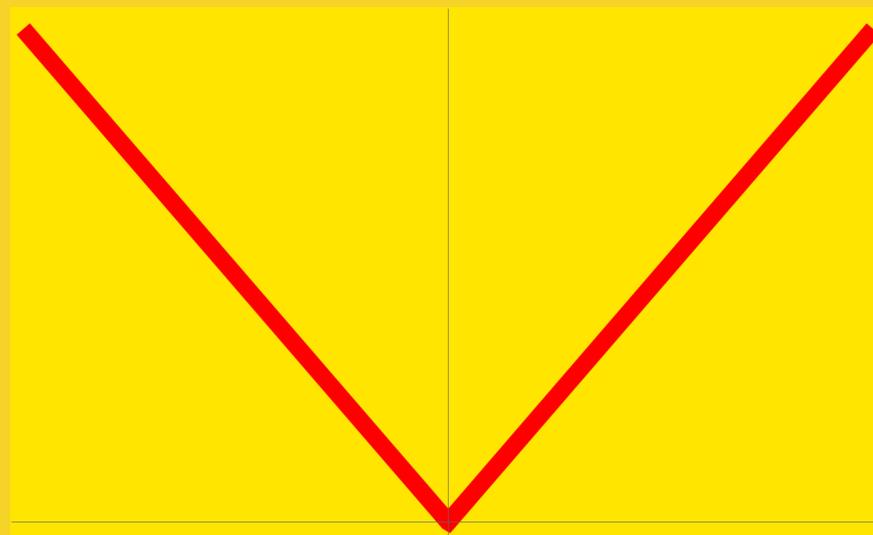
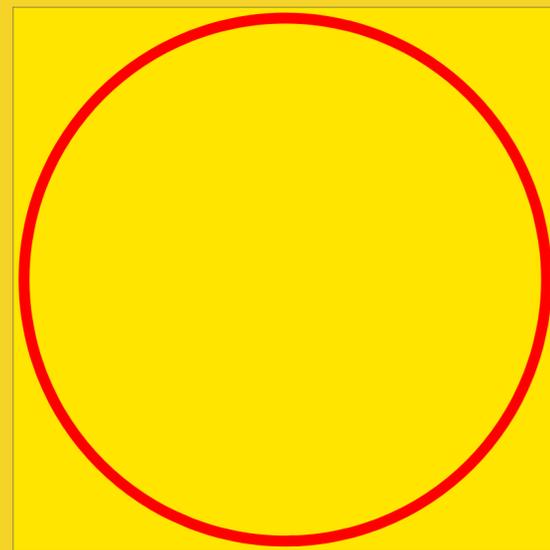
All you need is

$$y = 1/x$$

$$x^2 + y^2 = 1$$

$$y = |x|$$

$$x = -|\sin(y)|$$



*MODELLING*

*BUNGEE JUMP*

# *GOLDENEYE*



# *YESMAN*







The World's  
**BUNGEE**

KAWAARU ZIP LINE  
BUNGEE 47M

The World's  
**BUNGEE**

**WORLD**

**KAWAARU ZIP LINE**

**Hasket**

*DAYLIGHT*

# DAYLIGHT TIME

```
days = DateRange[{2019, 1, 1}, {2020, 1, 1}, {5, "Day"}];  
A = Sunrise[days]; B = Sunset[days];  
S1 = DateListPlot[  
  TimeSeriesThread[UnitConvert[#[[2]] - #[[1]], "Hour"] &, {A, B}]]  
S2 = Plot[12.1 + 3 Sin[x - Pi/2 + 0.2], {x, 0, 2 Pi}]
```

$$f(x) = 12 - 3 \cos(x)$$

