

# INTRODUCTION TO CALCULUS

MATH 1A

UNIT 13: WORKSHEET

## Hospital's rule

**1:** Compute the limit:

$$\lim_{x \rightarrow 0} \frac{\sin(3x) + x}{x^2 + x}$$

**2:** Compute the limit:

$$\lim_{x \rightarrow 1} (x - 1) / \log(x - 1)$$

**3:** Find the limit:

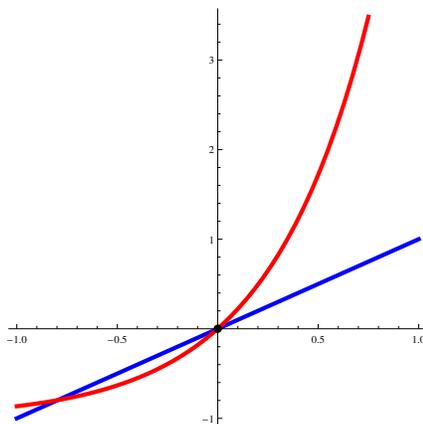
$$\lim_{x \rightarrow \infty} \log(7x + 3) / \log(9x + 4)$$

**4:** Find the limit (see Figure 1 below)

$$\lim_{x \rightarrow 0} \frac{\exp(2x) - 1}{x} ?$$

**5:** Find the limit

$$\lim_{x \rightarrow -1} (x^2 + 2x + 1) / (x + 1) .$$

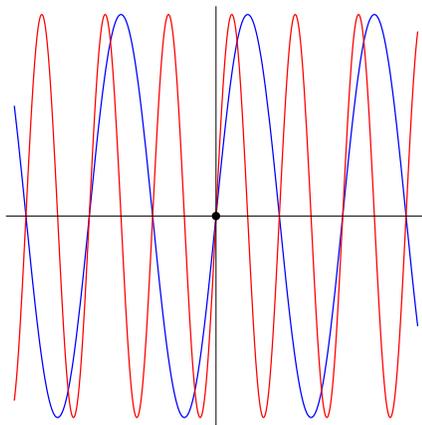


The functions  $\exp(2x) - 1$  and  $x$ .

**5:** Apply l'Hospital's rule to get the limit of

$$f(x) = \frac{\sin(200x)}{\sin(300x)}$$

for  $x \rightarrow 0$ .



**7:** What does l'Hospital's rule tell about the limit

$$f(x) = \frac{\sin(200x)}{\sin(300x)}$$

for  $x \rightarrow \infty$ .

**8:** What does l'Hospital's rule tell about the limit

$$f(x) = \frac{\cos(200x)}{\cos(300x)}$$

for  $x \rightarrow 0$ .