

## Lecture 1: Worksheet

In this first lecture, we want to see that the **essence** of calculus is already in **basic arithmetic**.

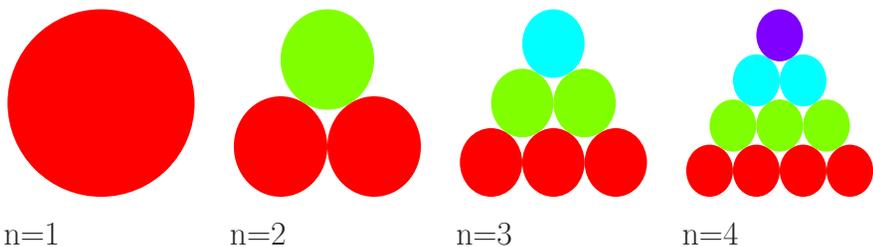
### Triangular numbers

We stack disks onto each other building  $n$  layers and count the number of discs. The number sequence we get are called **triangular numbers**.

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1 3 6 10 15 21 36 45 ...

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This sequence defines a **function** on the natural numbers. For example,  $f(4) = 10$ .

- 1 Can you find  $f(100)$ ? The task to find this number was given to Carl Friedrich Gauss in elementary school. The 7 year old came up quickly with an answer. How?



Carl-Friedrich  
Gauss, 1777-1855

### Tetrahedral numbers

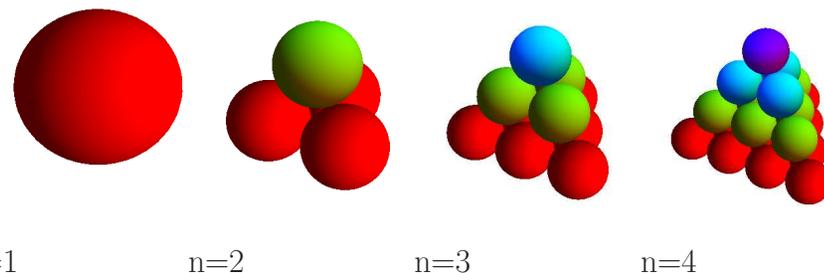
We stack spheres onto each other building  $n$  layers and count the number of spheres. The number sequence we get are called **tetrahedral numbers**.

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1 4 10 20 35 56 84 120 ...

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Also this sequence defines a **function**. For example,  $g(3) = 10$ . But what is  $g(100)$ ? Can we find a formula for  $g(n)$ ?



- 2 Once you know the formula for  $g(n)$  given to you as  $g(n) = n(n+1)(n+2)/6$ , verify that it is the right one, by checking  $g(n) - g(n-1) = n(n+1)/2$ .