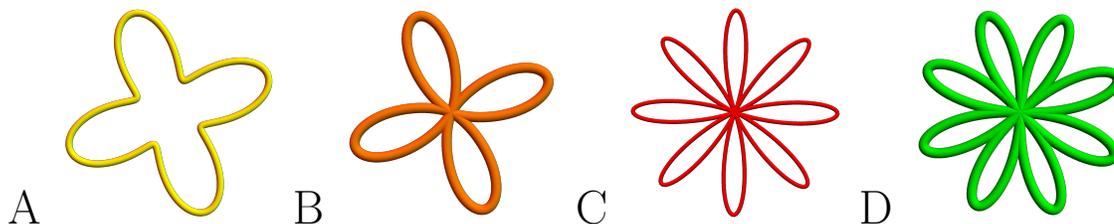


Homework 7: Polar coordinates

This homework is due Wednesday, 9/25.

- 1 a) Change to polar coordinates: $(x, y) = (2, -2\sqrt{3})$.
 b) Change to Cartesian coordinates: $(r, \theta) = (3, \pi/2)$
 c) Change to cylindrical coordinates: $(x, y, z) = (-3\sqrt{3}, 3, 27)$
 d) Change to Cartesian coordinates $(r, \theta, z) = (7, 3\pi/4, -11)$

- 2 Match the following curves with the formula giving them in polar coordinates



Formula	Enter A-D
$r = \sin(4\theta) $	
$r = 2 + \sin(4\theta)$	
$r = \cos^2(4\theta)$	
$r = 1 + \sin(4\theta)$	

- 3 a) The polar curve $r = |\sin(21\theta)|$ is called a rose. How many petals does it have?
 b) Identify the surface given in cylindrical coordinates as $r^2 = 1 + (z - 5)^2$.
 c) Write the hyperboloid $x^2 + y^2 - (z - 1)^2 = 4$ in cylindrical coordinates.
 d) Identify the surface $2r^2 - z = -1$.

- 4 a) Identify the surface whose equation is given in cylindrical coordinates as

$$\cos(\theta) + \sin(\theta) = 1/r .$$

- b) Write the ellipsoid $x^2/4 + y^2/9 + z^2/16 = 1$ in cylindrical coordinates.

- 5 Use the Mathematica command "RevolutionPlot3D" to plot the surface which is given by

$$z = (\sin(7\theta) + \cos(7\theta))e^{-r^2} .$$

(See example Mathematica command below. As usual, you can print the result out and include in the homework.)

Example:

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RevolutionPlot3D [t, {r, 0, 1}, {t, 0, 2 Pi}]
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Main definitions

A point (x, y) in the plane has **polar coordinates** $r = \sqrt{x^2 + y^2} \geq 0, \theta = \arctan(y/x)$. Important is the relation $(x, y) = (r \cos(\theta), r \sin(\theta))$. To get the angle, it is custom to chose arctan values in $(-\pi/2, \pi/2]$ and add π if $x < 0$ or $x = 0, y < 0$. This gives a value in $\theta \in [0, 2\pi)$. A point (x, y, z) in space has the **cylindrical coordinates** (r, θ, z) , where (r, θ) are the polar coordinates of (x, y) . A curve given in polar coordinates as $r(\theta) = f(\theta)$ is called a **polar curve**. It can in Cartesian coordinates be described as $\vec{r}(t) = [f(t) \cos(t), f(t) \sin(t)]$.