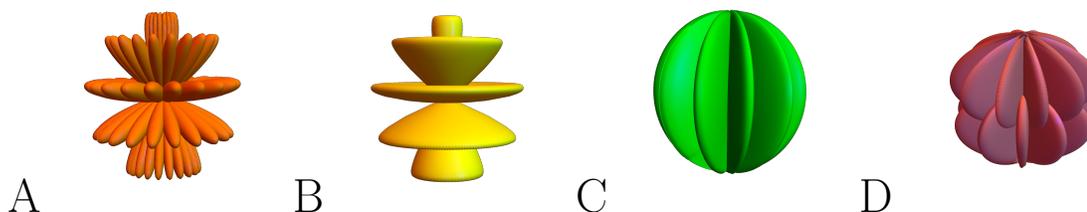


Homework 8: Spherical coordinates

This homework is due on Friday, 9/27.

- 1 a) Change to spherical coordinates $(x, y, z) = (-5\sqrt{3}, 0, 5)$.
 b) Change to spherical coordinates $(x, y, z) = (-1, -1, \sqrt{2})$.
 c) Change to Cartesian coordinates $(\rho, \phi, \theta) = (2, \pi/2, \pi/2)$.
 d) Change to spherical coordinates $(r, \theta, z) = (3, \pi/2, 3\sqrt{3})$.
- 2 Match the surfaces with the expressions given in spherical coordinates



Formula $\rho = \dots$	Enter A-D
$\sin(10\phi)$	
$\cos(10\theta) + \sin(10\phi)$	
$1 + \cos(10\theta)$	
$\sin(10\theta)\phi$	

- 3 a) Identify the surface given in spherical coordinates as $\sin(\phi) = 2\cos(\phi)$.
 b) Write $\sin^2(\phi) + \cos^2(\phi)/4 = 1/\rho^2$ in Cartesian coordinates.
 c) What is the name of the surface $\cos(\phi) + 1/\rho = \rho\sin^2(\phi)$.
- 4 a) Identify the surface given in spherical coordinates as

$$\rho^2(\sin^2(\phi)\sin^2(\theta) + \cos^2(\phi)) = 16.$$

- b) Write $\rho(\rho\sin^2(\phi) + \cos(\phi)) = 16$ in cylindrical coordinates and name it.

- 5 Here is an other opportunity to befriend quadrics. Please chose a simple example in each case (not to torture the grader).
- Write the sphere in spherical coordinates.
 - Write the cone in spherical coordinates.
 - Write the cylinder in spherical coordinates.
 - Write the one-sheeted hyperboloid in spherical coordinates.
 - Write the two-sheeted hyperboloid in spherical coordinates.
 - Write the elliptic paraboloid in spherical coordinates.
 - Write the hyperbolic paraboloid in spherical coordinates.
- 6 a) Use the Mathematica command "SphericalPlot3D" to plot a bumpy sphere

$$\rho(\phi, \theta) = (2 + \cos(3\phi) + \sin(5\theta)) .$$

with $0 \leq \phi \leq \pi$ and $0 \leq \theta < 2\pi$.

b) Now change the function a bit and create your own surface different from anything above. Already practice a bit of creativity.

Main definitions

Spherical coordinates use the distance $\rho \geq 0$ to $(0, 0, 0)$ as well as two angles θ and ϕ . The angle $\theta \in [0, 2\pi)$ is the polar angle in the xy -coordinates and $\phi = [0, \pi]$ is the angle between \vec{OP} and the z -axis. We have:

$$x = \rho \sin(\phi) \cos(\theta)$$

$$y = \rho \sin(\phi) \sin(\theta)$$

$$z = \rho \cos(\phi) .$$