

*Lecture 11*

*Vectors*

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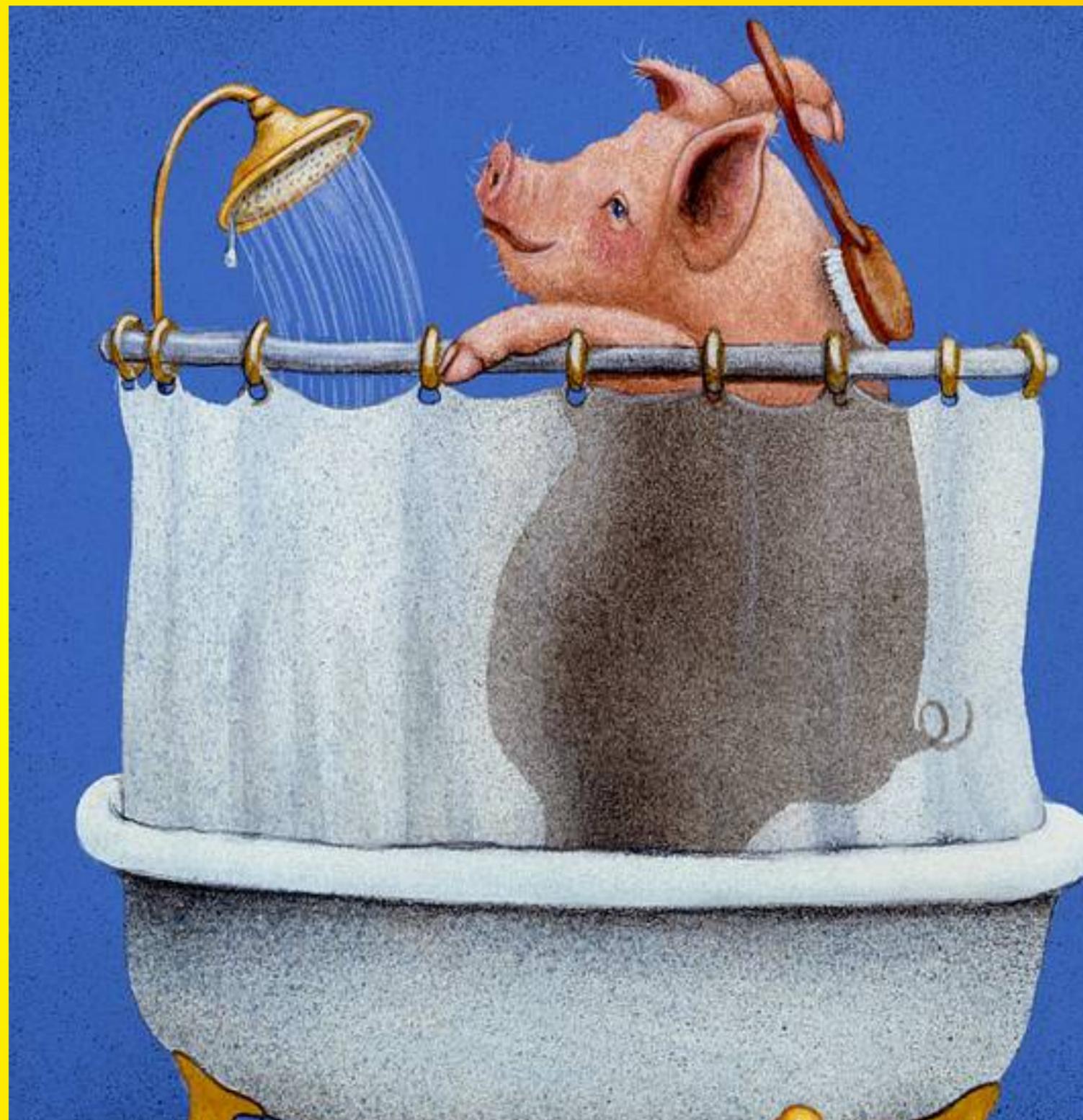
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*What is a vector?*

A quantity with  
magnitude and  
direction?

*Hog  
wash!*



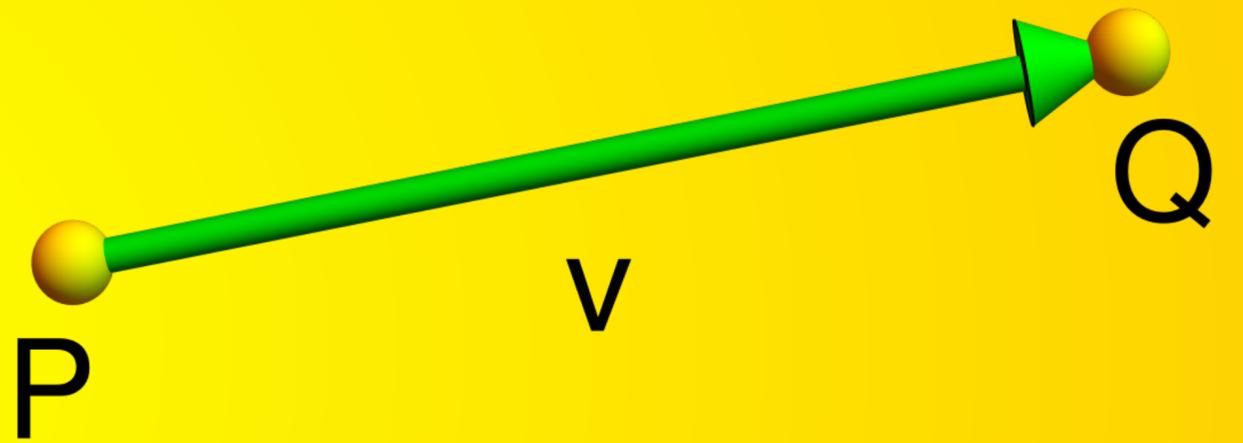


A movie is a vector  
because it has a  
magnitude and  
direction !

$\langle 0,0,0 \rangle$  is not a vector with that definition because it has no direction.

In reality,  $\langle 0,0,0 \rangle$  is a very important vector.

*What is a vector?*



Two points like

$P=(1,1,1), Q=(3,4,5)$

define a vector  $\langle 2,3,4 \rangle$

# *Notation*

$$\vec{i} = \langle 1, 0, 0 \rangle$$

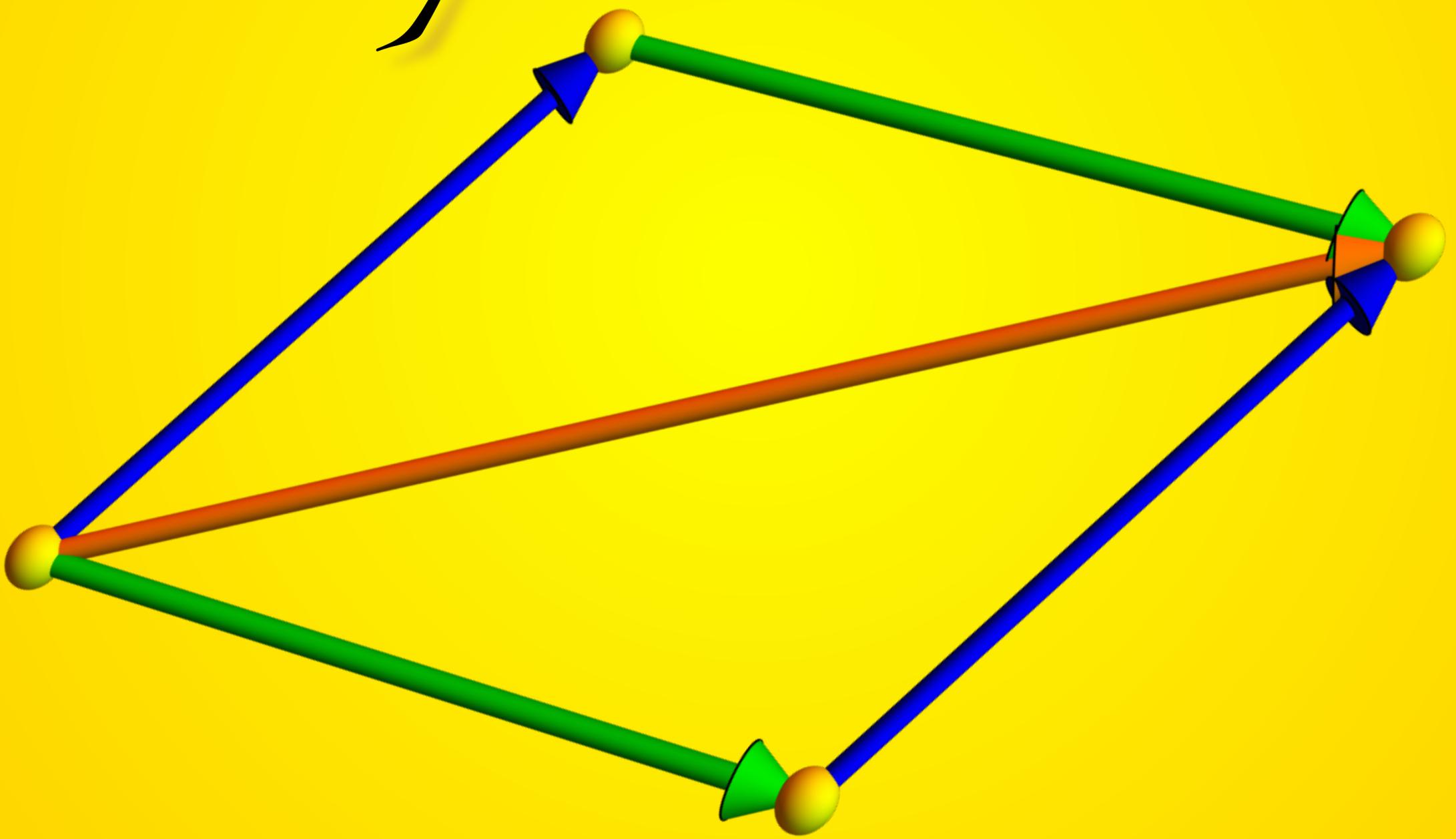
$$\vec{j} = \langle 0, 1, 0 \rangle$$

$$\vec{k} = \langle 0, 0, 1 \rangle$$

What did the vector say  
after making a bad joke?

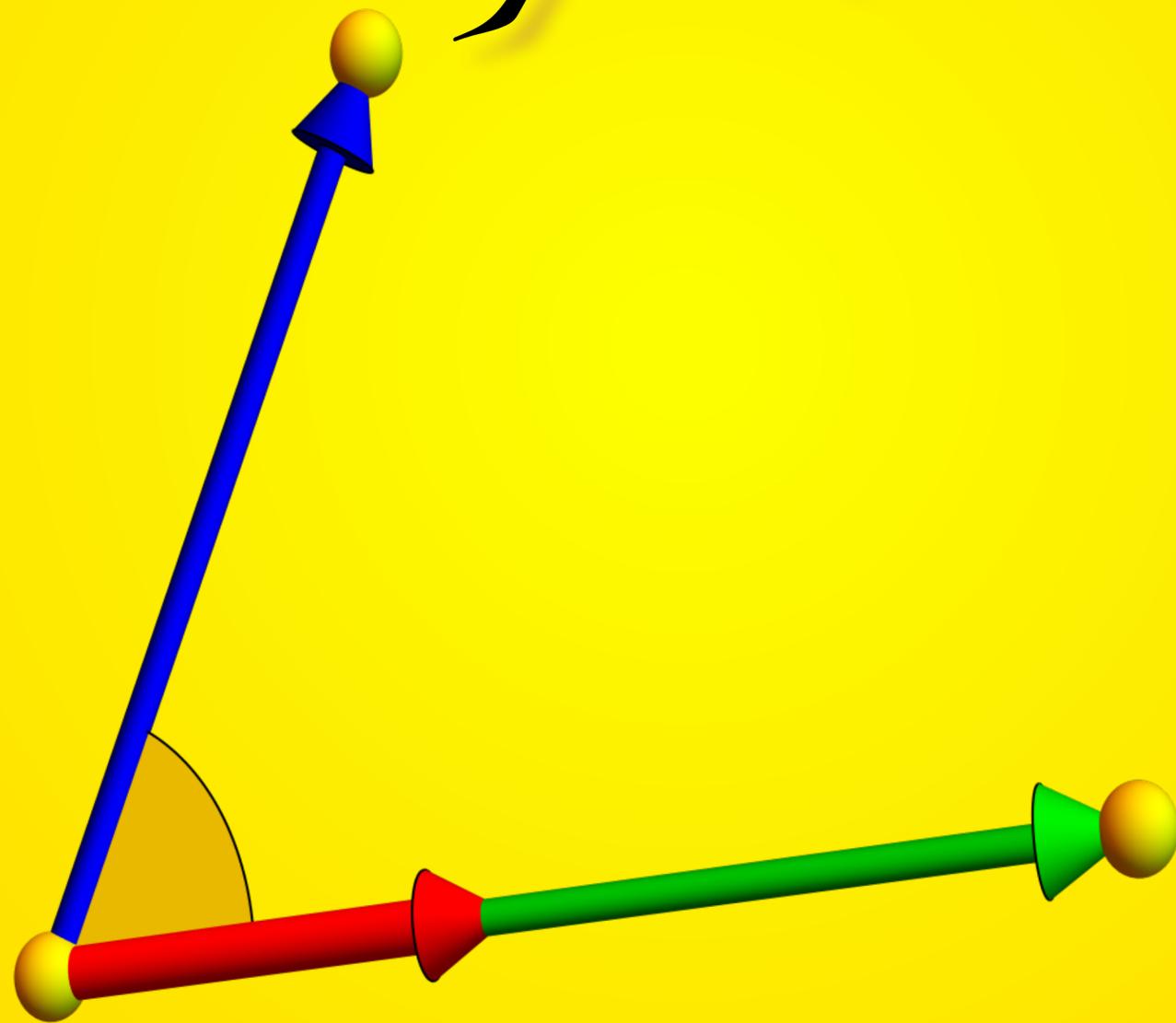
i j k'ed

# *Operations*



Vectors  $v$  and  $w$  are at a party. Vector  $v+w$  comes in and asks "Can I join"  
 $v$  and  $w$  reply: "Yes, it is now a closed party."

# Scalar projection



# Cases

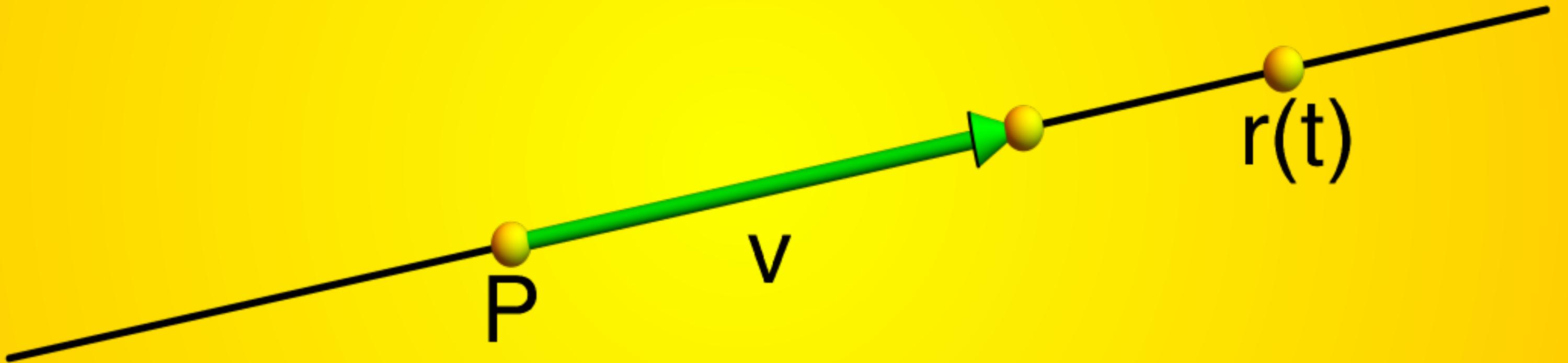
$$\text{comp}_{\vec{v}}(\vec{v}) = \|\vec{v}\|$$

If  $v, w$  are perpendicular, then  $\text{comp}_{\vec{w}}(\vec{v}) = 0$

$$\text{comp}_{\langle 1,0,0 \rangle}(\langle a, b, c \rangle) = a$$

$$\text{comp}_{\vec{v}}(\langle 0,0,0 \rangle) = 0$$

# *Lines*

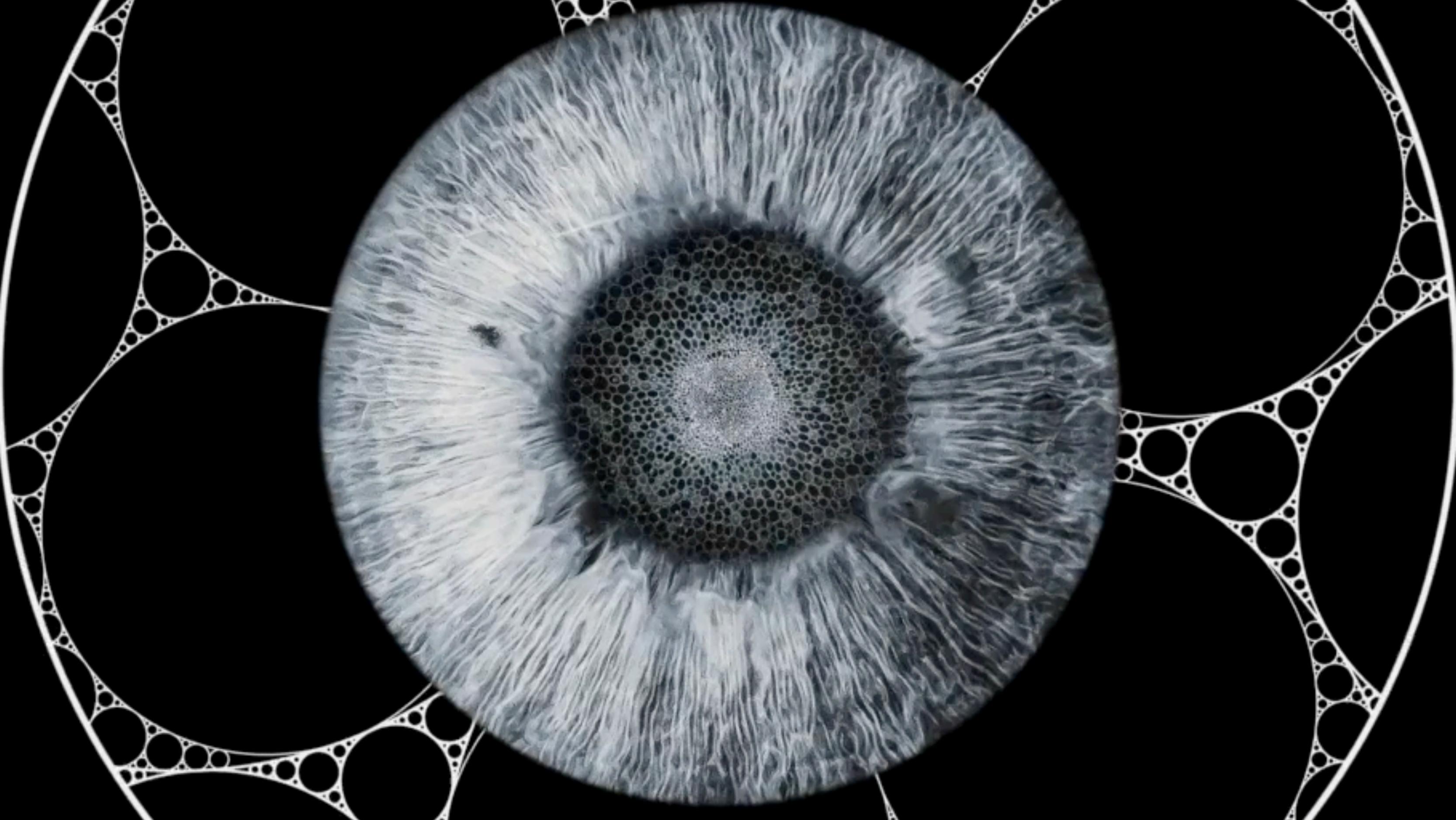


# *Lines*

I dabbled in Cartesian coordinates, but vector geometry is where I draw the line!

*Is space continuous?*

I dabbled in Cartesian coordinates, but vector geometry is where I draw the line.



Homework

due Friday

*THE END*