

Lecture 7: Quiz

Name:

Problem 1

Which of the following sets have the same cardinality as the interval $[0, 1]$?

- The two dimensional plane
- The three dimensional space
- The rational numbers.
- The complex numbers.
- The algebraic numbers.

Problem 2

Which two set operations are the addition and multiplication in a Boolean ring?

- intersection and union
- intersection and symmetric difference
- intersection and complement
- union and complement

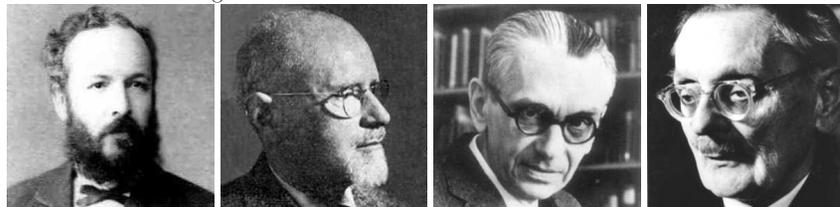
Problem 3

Which mathematician established first that there are different types of infinities. Infinities one can count and infinities which one can not count.

- Alan Turing
- Georg Cantor
- Alfred Tarski
- Kurt Goedel

Problem 4

Which of the following mathematicians is Kurt Goedel?



a)

b)

c)

d)

Problem 5

The Continuum Hypothesis (CH) tells that

- There exists a cardinality larger than the cardinality of the reals and the cardinality of the integers.
- There exists a cardinality different from the cardinality of the integers.
- There exists an infinite set.
- There does not exist any cardinality smaller than the cardinality of the reals and larger than the cardinality of the integers.

Problem 6

Which properties hold in a Boolean ring with addition $+$ and multiplication \cdot ? Remember that for sets the addition is the symmetric difference and the multiplication is the intersection.

- $A \cdot A = \emptyset$
- $A \cdot A = A$
- $A + A = A$
- $A + A = A \cdot A$
- $A + A = \emptyset$.

Problem 7

Which of the following paradoxa have been found by Russell:

- The Berry paradox about the smallest integer which can be described in 10 sentences.
- The liars paradox: I'm a liar.
- The set of all sets which do not contain themselves as a set.
- There is a surprise examination this year.
- The barber's paradox: the barber shaves everybody who does not shave himself.